



# RESEARCH REPORT

SURVO 84

Interactive system for statistical computing,  
graphics and text processing

BY

Seppo Mustonen

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DEPARTMENT OF STATISTICS  
UNIVERSITY OF HELSINKI  
SF 00100 HELSINKI 10 FINLAND

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**SURVO 84 - interactive system for statistical computing,  
graphics and text processing**

**Seppo Mustonen**

**Department of Statistics  
University of Helsinki  
Aleksanterinkatu 7  
00100 Helsinki 10  
Finland**

## SURVO 84 - interactive system for statistical computing, graphics and text processing

SURVO 84 is an integrated interactive statistical system for statistical computing. SURVO 84 also includes many supporting functions in text processing, graphics and mathematics for such users who need a handy workstation for various practical tasks occurring in their work.

All the activities in SURVO 84 are controlled from the SURVO 84 EDITOR which is a general text processing program. Besides standard word processing this editor provides several enhancements not encountered in typical text processing systems.

SURVO 84 can also be compared with spreadsheet programs to some extent. However, in SURVO 84 the calculations take place in the edit field which simultaneously is the basis for text processing, graphics and all other functions. In the edit field the user can control each character separately. In spreadsheet programs it is typical that some larger unit like 'number' or 'word' is the smallest representable entity.

We call our approach editorial mode. The idea of editorial mode was introduced in SURVO 76 which is an interactive statistical system for the Wang 2200 series. The present version of SURVO 84 runs on Wang PC.

### Working with SURVO 84

The edit field is like a notebook for the user. He/she can write text and numbers in any place. Text and numerical tables are edited by function keys and editing commands.

Also information from various files (for instance, from any text file) can be moved to the edit field for editing and processing. Furthermore SURVO 84 provides data files for larger data sets which are needed, for example, in statistical analysis. Also many activities required in data base management are available.

The results of various computational operations are immediately displayed in the edit field, but they may also be directed to output files or to the printer.

A very essential feature in SURVO 84 is that all commands and operations are also written in the edit field. An operation is activated by moving the cursor to the operation line and by pressing the COMMAND key. Since the operations reside among the text, it is simple to edit and reactivate them. Unnecessary operations can, of course, be immediately erased.

From various commands and operations the users can build programs for their applications. We call these programs work schemes, since they get their guidance not only from operations, but also from

various keywords and specifications written around the program in the same edit field. The user maintains work schemes like any text and stores them with the edit field. Typical small work schemes will be shown at the end of this paper.

### SURVO 84 operations

SURVO 84 includes now (August 1984) about 200 operations from the following areas:

1. Text editing and control of the edit field
2. Data management
3. Mathematics
  - Simple arithmetics and evaluation of numerical expressions
  - Arithmetics with numerical tables
  - Special 'Touch mode' for arithmetics and calculation with tables
  - Matrix operations (an extensive matrix interpreter)
  - Evaluation of symbolic derivatives
4. Graphics
  - Bar charts (8 different types)
  - Pie charts, Matrix diagrams, Age pyramids
  - Histograms and fitting of statistical distributions
  - Scatter diagrams (correlation diagrams)
  - Time series plots and line graphs
  - Probability plots (normal distribution)
  - Curves and families of analytic curves
  - Representation of multivariate data (Chernoff's faces, Andrews' function plots)
5. Statistical analysis
  - Basic statistics, frequency distributions and tables
  - Transformation of variables
  - Data sorting and order statistics
  - Linear and non-linear regression analysis
  - Correlations, principal components and factor analysis
  - Discriminant analysis and canonical correlations (with the matrix interpreter)
6. Simulation
  - Generating artificial data according to statistical models

### Documentation

All documentation of SURVO 84 is based on a dynamic inquiry system. It is a fundamental part of SURVO 84 and always easily accessed without losing contact to the current job. During queries information and examples are displayed in a temporary window. When desired, that information may be loaded to the edit field or printed on paper.

SURVO 84 can also be used in a special tutorial mode which permits saving of each key stroke in a tutor file. Such a tutor file may be edited with the SURVO 84 EDITOR and various sessions with SURVO 84 can be repeated step by step under the control of tutors. Teaching programs for SURVO 84 and its applications can be made in tutorial mode.

## Hardware requirements

The present SURVO 84 version can be run on Wang PC with a 256KB memory, a medium resolution graphics card and a 10MB Winchester. In graphics SURVO 84 supports the EPSON RX printers and SERVOGOR 281 and 284 plotters. SURVO 84 includes over 250 program modules and system files which require space over 2MB on the Winchester disk.

## Examples

On the following pages 48 typical SURVO 84 applications are presented. Although we have tried to give a cross section of the current SURVO 84 functions, not all features are included. For example, some topics related to table and file management, especially 'touch mode', are not covered, since paper is too rigid a medium for showing these dynamic actions.

Each example is illustrated with two exhibits. The first one usually describes the situation in the edit field before activation of a certain operation or a series of operations. The second one tells what is seen on the screen after the operations have been completed. The activated lines are always displayed in reversed mode.

SURVO 84 EDITOR displays continuously the current date and time on the top line. In this case the time elapsed between two consecutive pictures does not tell anything about the speed, since each hard-copy took time over 6 minutes + a random time depending on the alertness of the author when preparing these examples.

The pictures are produced by the hardcopy utility of SURVO 84 on the EPSON RX-80 printer or on the SERVOGOR 281 plotter. Most of the exhibits have been reduced by 50 per cent in scale before printing. The text is printed by the PRINT operation of SURVO 84 on the same printer.

TRIM is a typical SURVO 84 operation for text editing.  
When hyphenating words, the simple rules of the Finnish language  
seem to work rather satisfactorily in other languages, too.  
SAVE TRIM on the first line in the edit field is an operation  
for saving the contents of the current edit field to file TRIM.

■ 9 1 SURVO 84 EDITOR 07-22-1984 15:30:56 A: 100 100 28580 0

1 \*SAVE TRIM  
2 \*  
3 \*  
4 \*  
5 \*TRIM3 55  
6 \* The line length in any text can be altered by a TRIM (or T) operation.  
7 \* It has various forms. We show the idea of TRIM by changing the line  
8 \*length of this chapter to 55. We use TRIM3 which allows the words to  
9 \*be splitted according to the rules of the Finnish language.  
10 \* In most cases the result is adequate for English, too. If not, it is  
11 \*easy to make adjustments by simple editing.  
12 \*  
13 \*  
14 \*  
15 \*  
16 \*  
17 \*  
18 \*  
19 \*  
20 \*  
21 \*  
22 \*  
23 \*

■ 9 1 SURVO 84 EDITOR 07-22-1984 15:38:46 A: 100 100 29752 0

1 \*SAVE TRIM  
2 \*  
3 \*  
4 \*  
5 \*TRIM3 55  
6 \* The line length in any text can be altered by a TRIM  
7 \*(or T) operation. It has various forms. We show the  
8 \*idea of TRIM by changing the line length of this chapter  
9 \*to 55. We use TRIM3 which allows the words to be split-  
10 \*ted according to the rules of the Finnish language.  
11 \* In most cases the result is adequate for English, too.  
12 \*If not, it is easy to make adjustments by simple edi-  
13 \*ting.  
14 \*  
15 \*  
16 \*  
17 \*  
18 \*  
19 \*  
20 \*  
21 \*  
22 \*  
23 \*

All the special display modes of the computer are supported by the SURVO 84 EDITOR. Some of them (like blinking) cannot be seen on paper.

The PRINT operation for making printouts on paper has several forms. Here the simplest one is employed. This document has been printed by using one PRINT operation.

```
■ 11 1 SURVO 84 EDITOR 08-17-1984 18:34:23          A: 100 100 27047 0
 1 *SAVE PRINT
 2 *
 3 *
 4 *
 5 *Text and tables in the edit field are printed on paper by a PRINT
 6 *operation.
 7 *
 8 *On the screen the current display mode is selected by one special
 9 *function key (F5:FORMAT), which gives in turn:
10 * 0 normal
11 * 1 bold           SURVO 84
12 * 2 subscript      A1,A2,...,An
13 * 3 superscript    X3+aX2+bx+c=0
14 * 4 underscore     SURVO 84
15 * 5 blinking
16 * 6 overscore
17 * 7 reversed video SURVO 84
18 *
19 *On the EPSON-RX printer also some display modes are supported.
20 *
21 *PRINT 5,19_
22 *
23 *
```

Text and tables in the edit field are printed on paper by a PRINT operation.

On the screen the current display mode is selected by one special function key (F5:FORMAT), which gives in turn:

0	normal	
1	bold	SURVO 84
2	subscript	A <sub>1</sub> ,A <sub>2</sub> ,...,A <sub>n</sub>
3	superscript	X <sup>3</sup> +aX <sup>2</sup> +bx+c=0
4	underscore	SURVO 84
5	blinking	SURVO 84
6	overscore	
7	reversed video	SURVO 84

On the EPSON-RX printer also some display modes are supported.

When data in tabular form is entered, it is not necessary to keep the columns aligned. A good order can be reached any time by using a FORM operation (here on line 5) which aligns the columns according to the masks on the image line 6.

---

# 13 1 SURVO 84 EDITOR 07-24-1984 10:33:30 A: 100 100 28957 0

1 \*SAVE FORM  
 2 \*  
 3 \*Table formatting by a FORM operation:  
 4 \*  
 5 \*FORM 11,22,6 / Lines 11-22 to be formatted according to line 6  
 6 \* XXXXXXXXXX 12.1 1.12 123.1 123.1 1.1  
 7 \*  
 8 \* Yearly consumption of various beverages per inhabitant  
 9 \* Country Coffee Tea Beer Wine Spirits  
 10 \* (kg) (kg) (1) (1) (1)  
 11 \*Italy 3.6 0.06 13.6 106.6 2.0  
 12 \*Portugal 2.2 0.03 27.5 89.3 0.9  
 13 \*Norway 9.4 0.19 43.5 3.1 1.8  
 14 \*Spain 2.5 0.03 43.6 73.2 2.7  
 15 \*France 5.2 0.10 44.5 104.3 2.5  
 16 \*Finland 12.5 0.15 54.7 7.6 2.7  
 17 \*Sweden 12.9 0.30 58.3 7.9 2.9  
 18 \*Switzerland 9.1 0.25 73.5 44.9 2.1  
 19 \*Holland 9.2 0.58 75.5 9.7 2.7  
 20 \*England 1.8 3.49 113.7 5.1 1.4  
 21 \*Denmark 11.8 0.41 113.9 10.4 1.7  
 22 \*Ireland 0.2 3.73 124.5 3.8 1.9  
 23 \*

---

# 13 1 SURVO 84 EDITOR 07-24-1984 10:41:10 A: 100 100 29765 0

1 \*SAVE FORM  
 2 \*  
 3 \*Table formatting by a FORM operation:  
 4 \*  
 5 \*FORM 11,22,6 / Lines 11-22 to be formatted according to line 6  
 6 \* XXXXXXXXXX 12.1 1.12 123.1 123.1 1.1  
 7 \*  
 8 \* Yearly consumption of various beverages per inhabitant  
 9 \* Country Coffee Tea Beer Wine Spirits  
 10 \* (kg) (kg) (1) (1) (1)  
 11 \* Italy 3.6 0.06 13.6 106.6 2.0  
 12 \* Portugal 2.2 0.03 27.5 89.3 0.9  
 13 \* Norway 9.4 0.19 43.5 3.1 1.8  
 14 \* Spain 2.5 0.03 43.6 73.2 2.7  
 15 \* France 5.2 0.10 44.5 104.3 2.5  
 16 \* Finland 12.5 0.15 54.7 7.6 2.7  
 17 \* Sweden 12.9 0.30 58.3 7.9 2.9  
 18 \* Switzerland 9.1 0.25 73.5 44.9 2.1  
 19 \* Holland 9.2 0.58 75.5 9.7 2.7  
 20 \* England 1.8 3.49 113.7 5.1 1.4  
 21 \* Denmark 11.8 0.41 113.9 10.4 1.7  
 22 \* Ireland 0.2 3.73 124.5 3.8 1.9  
 23 \*

As a simple example of table management, sorting according to a certain column in the table is performed.

Here the countries are sorted in ascending order with respect to 'Wine consumption' by activating a SORT operation on line 25.

The mask '11111' on the image line tells the sort key.

To sort the countries in descending order, it is enough to change word 'SORT' to '-SORT' and activate again.

```

■ 14 1 SURVO 84 EDITOR 07-24-1984 10:50:36          A: 100 100 28468 0
7 *
8 * Yearly consumption of various beverages per inhabitant
9 * Country   Coffee   Tea    Beer   Wine  Spirits
10 *          (kg)    (kg)   (l)    (l)   (l)
11 * Italy     3.6     0.06   13.6  106.6  2.0
12 * Portugal  2.2     0.03   27.5  89.3   0.9
13 * Norway   9.4     0.19   43.5   3.1   1.8
14 * Spain    2.5     0.03   43.6  73.2   2.7
15 * France   5.2     0.10   44.5  104.3  2.5
16 * Finland  12.5    0.15   54.7   7.6   2.7
17 * Sweden   12.9    0.30   58.3   7.9   2.9
18 * Switzerland 9.1    0.25   73.5  44.9   2.1
19 * Holland  9.2     0.58   75.5   9.7   2.7
20 * England  1.8     3.49  113.7   5.1   1.4
21 * Denmark  11.8    0.41  113.9  10.4   1.7
22 * Ireland  0.2     3.73  124.5   3.8   1.9
23 *           11111
24 *
25 *SORT 11,22,23 / Sorting lines 11-22 according to image line 23
26 *
27 *
28 *
29 *

```

```

■ 14 1 SURVO 84 EDITOR 07-24-1984 10:58:21          A: 100 100 29684 0
7 *
8 * Yearly consumption of various beverages per inhabitant
9 * Country   Coffee   Tea    Beer   Wine  Spirits
10 *          (kg)    (kg)   (l)    (l)   (l)
11 * Norway   9.4     0.19   43.5   3.1   1.8
12 * Ireland  0.2     3.73  124.5   3.8   1.9
13 * England  1.8     3.49  113.7   5.1   1.4
14 * Finland  12.5    0.15   54.7   7.6   2.7
15 * Sweden   12.9    0.30   58.3   7.9   2.9
16 * Holland  9.2     0.58   75.5   9.7   2.7
17 * Denmark  11.8    0.41  113.9  10.4   1.7
18 * Switzerland 9.1    0.25   73.5  44.9   2.1
19 * Spain    2.5     0.03   43.6  73.2   2.7
20 * Portugal  2.2     0.03   27.5  89.3   0.9
21 * France   5.2     0.10   44.5  104.3  2.5
22 * Italy    3.6     0.06   13.6  106.6  2.0
23 *           11111
24 *
25 *SORT 11,22,23 / Sorting lines 11-22 according to image line 23
26 *
27 *
28 *
29 *

```

A typical bar chart is made from the data given in the edit field. Observe that, for example, scaling on the X axis is automatically selected by the PLOT operation on the basis of the data values. Also shadings for different age groups are chosen by the system. All these details can, of course, be determined by the user by entering proper specifications.

```

12 1 SURVO 84 EDITOR 07-21-1984 15:58:41 A: 100 72 31830 0
1 * DATA NORDIC,A,B,M
2 M Country _0-14 15-24 25-44 45-64 65-
3 A Sweden 841 571 1188 930 585
4 * Denmark 564 385 731 537 308
5 * Finland 506 399 727 468 202
6 * Norway 474 316 534 442 251
7 B Iceland 32 22 29 20 10
8 *
9 *HEADER=(2,3),Males_in_age_groups_(1000) LEGEND=Age: GRID=1000 TICK=100
10 *HOME=70,0 SIZE=729,300 YDIV=70,180,50
11 *PLOT NORDIC
12 *
13 *
14 *
15 *
16 *
17 *
18 *
19 *
20 *
21 *
22 *
23 *

```

```

12 1 SURVO 84 EDITOR 07-21-1984 16:26:25 A: 100 72 33073 0
1 * DATA NORDIC,A,B,M
2 M Country _0-14 15-24 25-44 45-64 65-
3 A Sweden 841 571 1188 930 585
4 * Denmark 564 385 731 537 308
5 * Finland 506 399 727 468 202
6 * Norway 474 316 534 442 251
7 B Iceland 32 22 29 20 10
8 *
9 *HEADER=(2,3),Males_in_age_groups_(1000) LEGEND=Age: GRID=1000 TICK=100
10 *HOME=70,0 SIZE=729,300 YDIV=70,180,50
11 *PLOT NORDIC
12 *
13 * Males in age groups (1000)
14 *
15 * Sweden
16 * Denmark
17 * Finland
18 * Norway
19 * Iceland
20 *
21 *
22 * 0 1000 2000 3000 4000 5000
23 * Age: 0-14  15-24  25-44  45-64  65- 

```

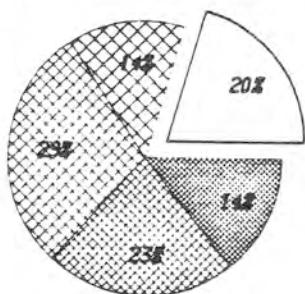
These pie charts are plotted on the SERVOGOR plotter (DEVICE=S).  
 The type of the graph is selected by TYPE=PIE.  
 The fills in various sectors are determined by SHADING where  
 numbers in parentheses refer to pens (colors).  
 The parameters given in parentheses in HEADER, for example,  
 refer to pen, letter size, letter height etc.

```

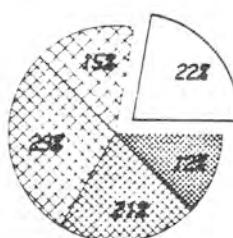
 15 1 SURVO 84 EDITOR 08-20-1984 14:15:37      A: 100 100 29804 0
 1 *
 2 *
 3 *DATA COUNTRIES,A,B,M
 4 M COUNTRY _0-14 15-24 25-44 45-64 65-
 5 A Sweden   841   571   1188   930   585
 6 * Denmark  564   385   731   537   308
 7 * Finland  506   399   727   468   202
 8 B Norway   474   316   534   442   251
 9 *
10 *PLOT COUNTRIES
11 *TYPE=PIE SHADING=0(1)P,2(2),4(2),6(2),8(2)
12 *VALUES=(1,30,25,1,2),MM%,7
13 *HEADER=(1,50,60,0,3),Males_in_age_groups
14 *DEVICE=S PEN=1,35,35,0,3
15 *
16 *
17 *
18 *
19 *
20 *
21 *
22 *
23 *

```

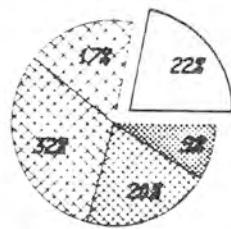
Males in age groups



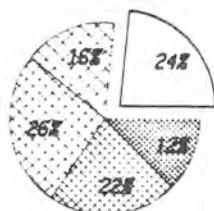
Sweden



Denmark



Finland



Norway

0-14 15-24 25-44 45-64 65-

One special form of bar charts in an age pyramid (TYPE=PYRAMID).

■ 13 1 SURVO 84 EDITOR 08-13-1984 18:15:54 A: 100 72 31839 0

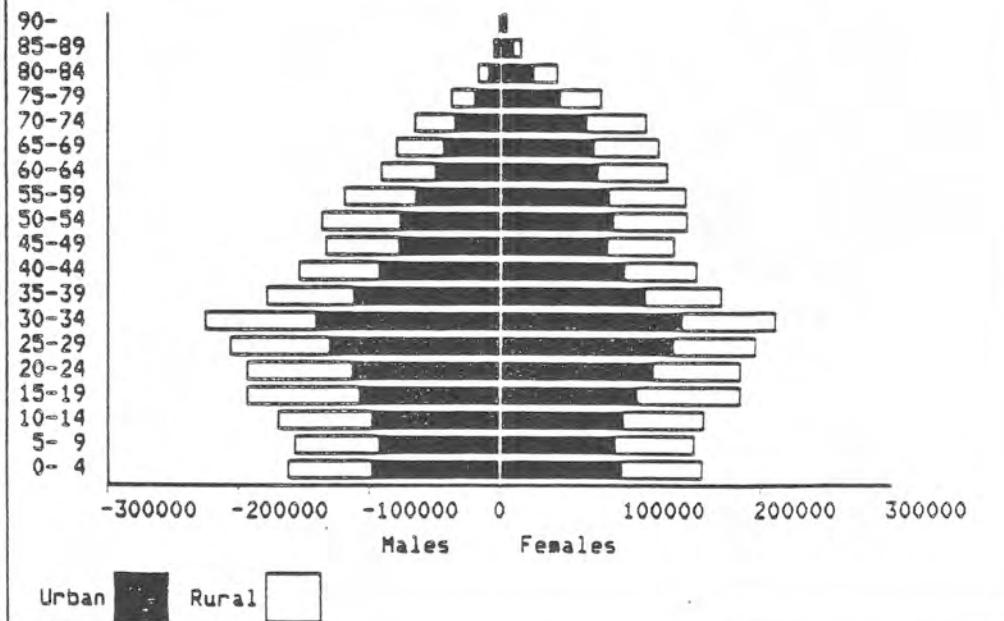
```

69 *HEADER=Age_pyramid_of_Finnish_population_in_1981
70 *PLOT FINLAND / TYPE=PYRAMID
71 *TEXT=SEX SEX=Males Females,275,70
72 *SHADING=0,10,10,0 HOME=70,0 SIZE=729,576 LEGEND=_ XDIV=79,600,100
73 *DATA FINLAND,X,Y,Z
74 *      Males          Females
75 Z Age   Urban     RuralI    Urban     Rural
76 X _0-_4  98297    64141    94036    61476
77 * _5-_9  92198    64997    87882    61428
78 * 10-14  97692    71849    94557    62239
79 * 15-19  107942   84661    105762   79183
80 * 20-24  113227   79993    116625   67403
81 * 25-29  129741   76574    132092   64212
82 * 30-34  140428   84486    138585   72422
83 * 35-39  111781   66638    110621   58569
84 * 40-44  92445    61069    94446    55852
85 * 45-49  77049    55753    81436    51374
86 * 50-54  76963    59786    85871    57149
87 * 55-59  65116    53909    83273    58700
88 * 60-64  49770    41449    74286    53148
89 * 65-69  43081    36557    70859    50219
90 * 70-74  34993    30922    65574    45777
91 * 75-79  19771    18630    45057    32336

```

■ 13 1 SURVO 84 EDITOR 08-13-1984 18:26:47 A: 100 72 33078 0

Age pyramid of Finnish population in 1981



A typical scatter diagram of two variables:

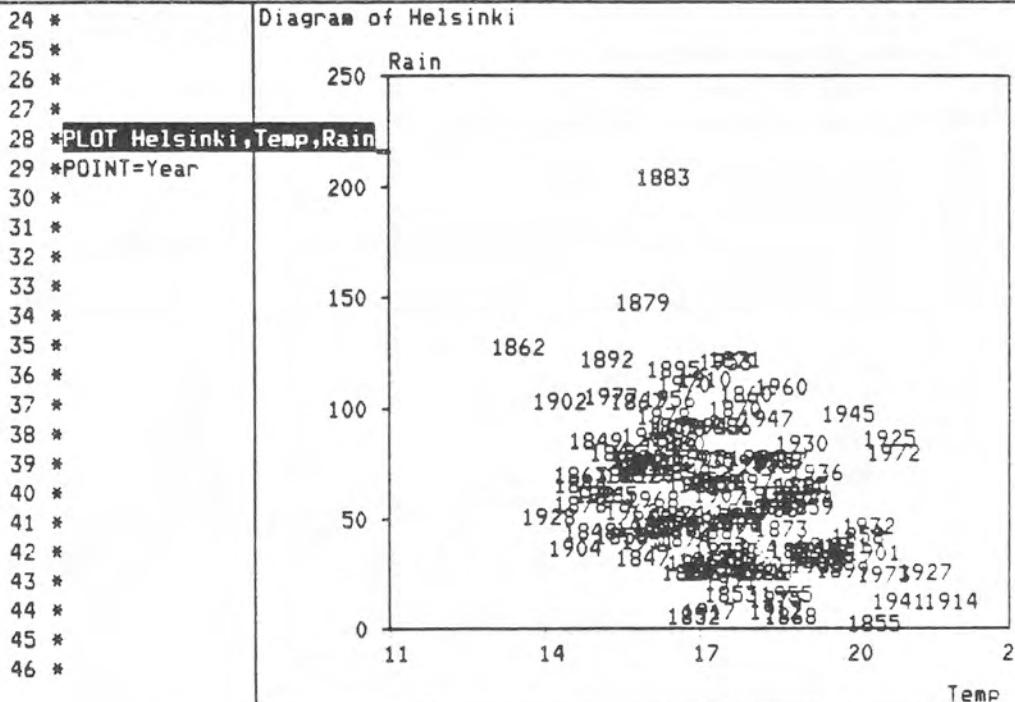
The correlation between rainfall and mean temperature in July for 135 consecutive years is displayed. Due to the specification POINT=Year each point in this scatter diagram is annotated by 'Year' thus giving possibility to detect exceptional years immediately. For example, summer of 1883 must have been extremely wet in Helsinki. The scalings are selected by the system.

■ 24 1 SURVO 84 EDITOR 07-22-1984 16:30:34 A: 100 72 31063 0

```

24 *
25 *
26 *
27 *
28 *PLOT Helsinki,Temp,Rain
29 *POINT=Year
30 *
31 *
32 *
33 *
34 *
35 *
36 *
37 *
38 *
39 *
40 *
41 *
42 *
43 *
44 *
45 *
46 *
```

■ 24 1 SURVO 84 EDITOR 07-22-1984 16:40:03 A: 100 72 32985 0



The mean temperature of July in Helsinki is plotted as a time series. The oscillations of the curve around a long term average (17.5 C) are characterized by a shading which is determined by the extra specification FILL.

---

■ 31 1 SURVO 84 EDITOR 07-23-1984 19:02:08 A: 100 72 32551 0

```

51 *
52 *PLOT Helsinki2,TIME(Year),Temp_
53 *DATA Helsinki2 IN Helsinki,101,135
54 *HEADER=Mean_temperature_in_Helsinki,_July_1944-78
55 *HOME=70,0 SIZE=729,400 YLABEL=Temperature_(C)
56 *LINE=1 GRID=XY XSCALE=1,7(5)32,35
57 *FILL=1,1,35,17.5 TICK=1,1
58 *
59 *
60 *
61 *
62 *
63 *
64 *
65 *
66 *
67 *
68 *
69 *
70 *
71 *
72 *
73 *

```

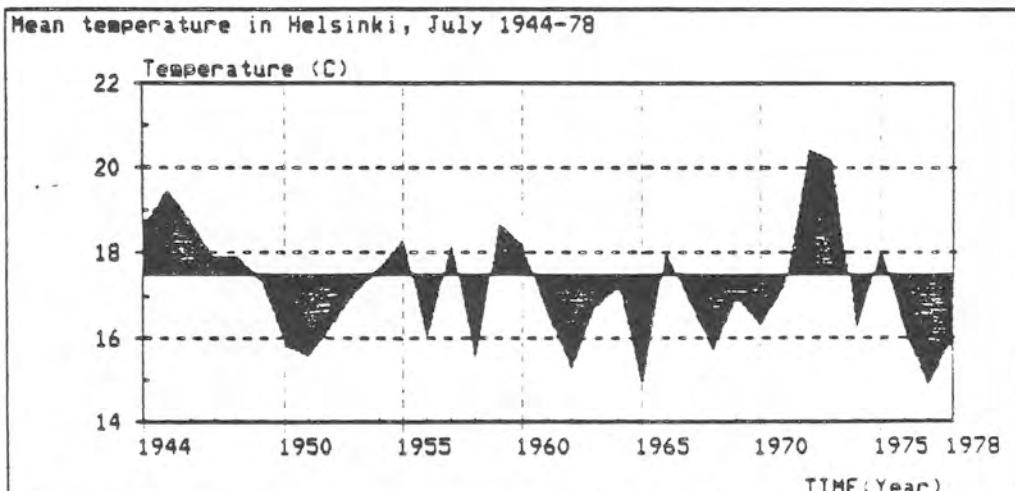
---

■ 31 1 SURVO 84 EDITOR 07-23-1984 19:12:17 A: 100 72 33000 0

```

51 *
52 *PLOT Helsinki2,TIME(Year),Temp_
53 *DATA Helsinki2 IN Helsinki,101,135
54 *HEADER=Mean_temperature_in_Helsinki,_July_1944-78
55 *HOME=70,0 SIZE=729,400 YLABEL=Temperature_(C)
56 *LINE=1 GRID=XY XSCALE=1,7(5)32,35
57 *FILL=1,1,35,17.5 TICK=1,1
58 * Mean temperature in Helsinki, July 1944-78
59 *
60 * Temperature (C)
61 *
62 *
63 *-----*
64 *-----*
65 *-----*
66 *-----*
67 *-----*
68 *-----*
69 *-----*
70 *
71 *
72 *
73 *

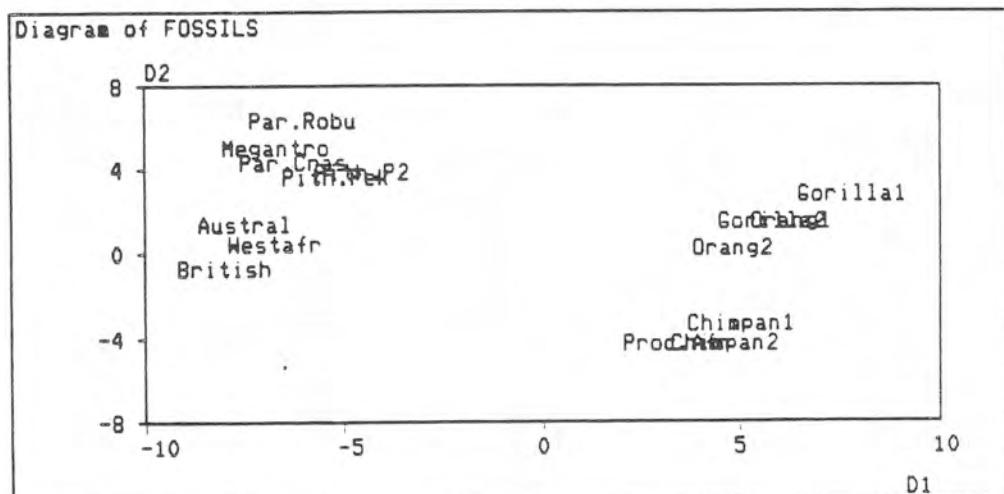
```



This and next two examples show, how interrelationships and structural differences in multidimensional data can be visualized. We have a data set of fossils, human races and apes. There are 8 measurements of the skull and teeth which have been transformed into 8 new variables by means of multiple discriminant analysis. First a simple scatter diagram of the two first discriminant functions D1,D2 is made. See how it separates apes and human races.

```
■ 19 1 SURVO 84 EDITOR 08-13-1984 19:41:14 A: 100 72 30285 0
1 *SAVE MULTI
2 *
3 *Plotting a scatter diagram
4 *PLOT FOSSILS,D1,D2 / POINT=Species HOME=70,0 SIZE=729,400
5 *
6 *DATA FOSSILS,X,Y,Z
7 Z Species D1 D2 D3 D4 D5 D6 D7 D8 Label
8 X Westafr -8.09 0.49 0.18 0.75 -0.06 -0.04 0.04 0.03 H1
9 * British -9.37 -0.68 -0.44 -0.37 0.37 0.02 -0.01 0.05 H2
10 * Austral -8.87 1.44 0.36 -0.34 -0.29 -0.02 -0.01 -0.05 H3
11 * Gorilla1 6.28 2.89 0.43 -0.03 0.10 -0.14 0.07 0.08 A1
12 * Gorilla2 4.28 1.52 0.71 -0.06 0.25 0.15 -0.07 -0.10 A2
13 * Orang1 5.11 1.61 -0.72 0.04 -0.17 0.13 0.03 0.05 A3
14 * Orang2 3.60 0.28 -1.05 0.01 -0.03 -0.11 -0.11 -0.08 A4
15 * Chimpan1 3.46 -3.37 0.33 -0.32 -0.19 -0.04 0.09 0.09 A5
16 * Chimpan2 3.05 -4.21 0.17 0.28 0.04 0.02 -0.06 -0.06 A6
17 * Pith.Pek -6.73 3.63 1.14 2.11 -1.90 0.24 1.23 -0.55 F1
18 * Pith.P2 -5.90 3.95 0.89 1.58 -1.56 1.10 1.53 0.58 F2
19 * Par.Robu -7.56 6.34 1.66 0.10 -2.23 -1.01 0.68 -0.23 F3
20 * Par.Cras -7.79 4.33 1.42 0.01 -1.80 -0.25 0.04 -0.87 F4
21 * Megantro -8.23 5.03 1.13 -0.02 -1.41 -0.13 -0.28 -0.13 F5
22 Y Proc.Afr 1.86 -4.28 -2.14 -1.73 2.06 1.80 2.61 2.48 F6
23 *
```

```
■ 19 1 SURVO 84 EDITOR 08-13-1984 19:50:32 A: 100 72 32815 0
1 *SAVE MULTI
2 *
3 *Plotting a scatter diagram
4 *PLOT FOSSILS,D1,D2 / POINT=Species HOME=70,0 SIZE=729,400
5 *
```



To get an overall picture of the entire set of 8 variables D1-D8, the face technique of Chernoff (1973) is used.

The variables D1-D8 are now connected to various features of the face according to the list given below the PLOT operation. See how the fossils resemble humans. The only exception is the mysterious 'Proconsul Africanus'.

The specification TYPE=FACES implies plotting of faces.

```

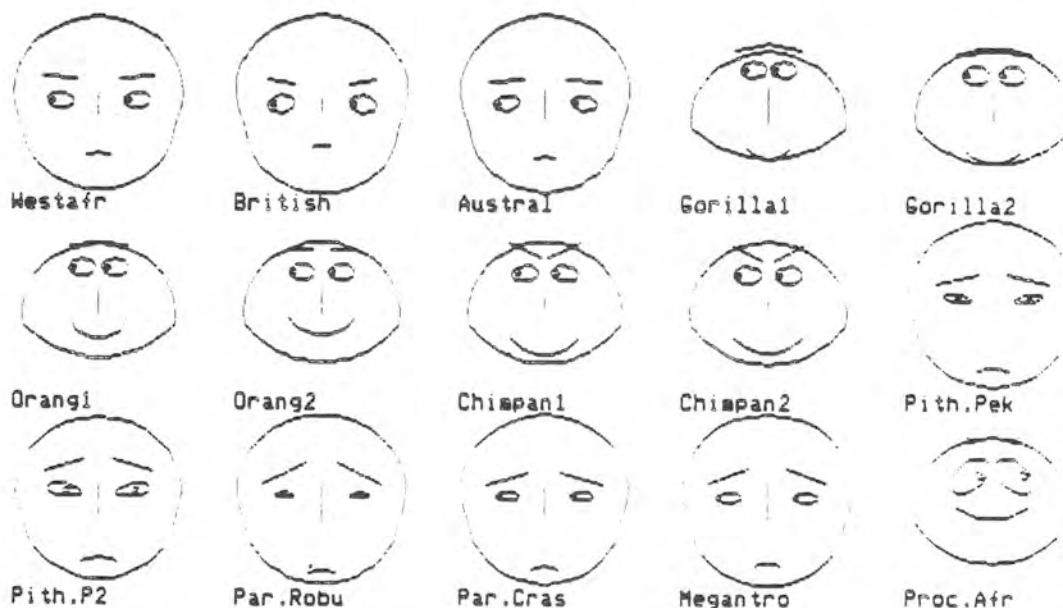
13 1 SURVO 84 EDITOR 07-21-1984 16:49:46      A: 100 72 31038 0
49 *HOME=0,0 SIZE=799,576 XDIV=0,799,0 YDIV=0,480,96
50 *PLOT FOSSILS / TYPE=FACES LABEL=Species FSIZE=160
51 *Specifications for Chernoff's faces of data FOSSILS
52 *VARIABLES: xmin      xmax      Features          fmin fmax
53 * -        0          0      Radius_to_corner_of_face_OP  0.6  1.0
54 * -        0          0      Angle_of_OP_to_horizontal   0.0  0.6
55 #01       6.28      -9.37    Vertical_size_of_face_OU   0.6  1.0
56 * -        0          0      Eccentricity_of_upper_face  0.5  1.5
57 * -        0          0      Eccentricity_of_lower_face  0.5  1.5
58 #02      -4.28      6.34      Length_of_nose            0.1  0.5
59 #03      -2.14      1.66    Vertical_position_of_mouth  0.2  0.8
60 #01      -9.37      6.28    Curvature_of_mouth_I/R     -4.0  4.0
61 #01      -9.37      6.28    Width_of_mouth           0.2  1.0
62 #01      -9.37      6.28    Vertical_position_of_eyes  0.0  0.4
63 #01       6.28      -9.37   Separation_of_eyes         0.3  0.8
64 #04      -1.73      2.11      Slant_of_eyes            -0.5  0.5
65 #05      -2.23      2.06    Eccentricity_of_eyes        0.3  1.0
66 #06      -1.01      1.8      Size_of_eyes             0.1  0.2
67 #07      -.28      2.61      Position_of_pupils        -0.1  0.1
68 #08      -.87      2.48    Vertical_position_of_eyebrows  0.2  0.4
69 #02      -4.28      6.34    Slant_of_eyebrows          -0.5  0.5
70 #03      -2.14      1.66    Size_of_eyebrows          0.1  0.5
71 *END of plotting specifications

```

```

1 1 SURVO 84 EDITOR 07-21-1984 17:01:38      A: 100 72 33023 0
Chernoff's faces of FOSSILS

```



Andrews' (1972) function plots for the same data.  
 Each observation D1,D2,...,D8 is represented by the function  
 $f(t)=D1/\sqrt{2}+D2\sin(t)+D3\cos(t)+D4\sin(2t)+\dots$   
 Due to the LABEL specification the curves can be labelled in  
 regular intervals by selected names (here variable 'Label').

```

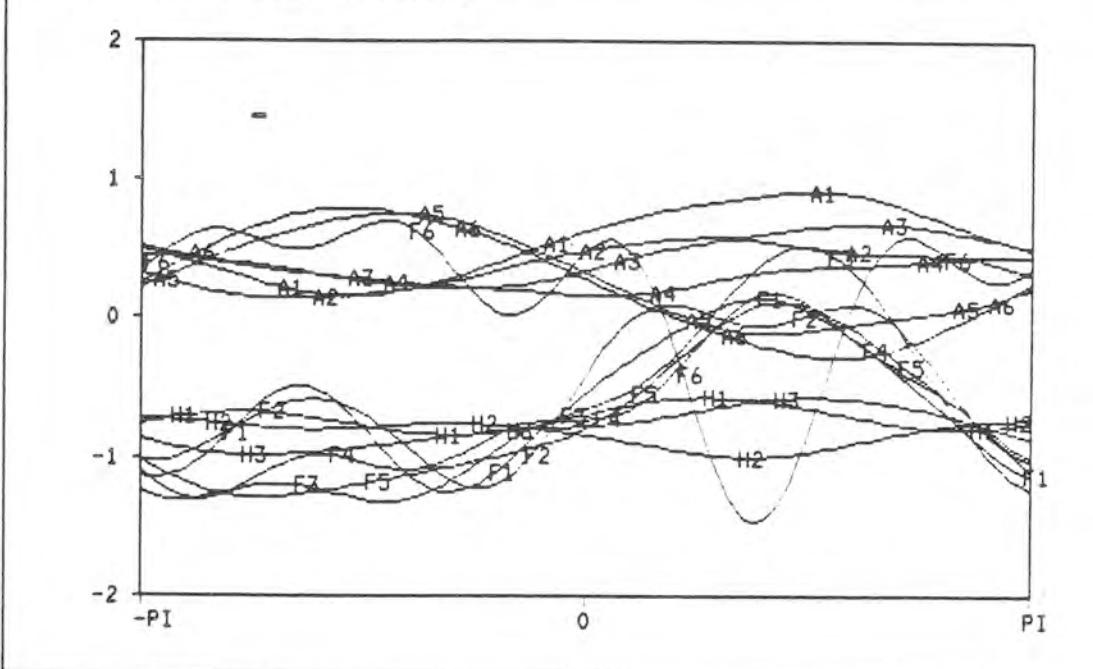
■ 13 1 SURVO 84 EDITOR 08-13-1984 19:58:48      A: 100 72 32331 0
72 *
73 *
74 *
75 *HOME=0,0 SIZE=799,576 CLEAR=TEXT
76 *PLOT FOSSILS / TYPE=ANDREWS SCALING=0,1 LABEL=Label
77 *Specifications for Andrews' function plots of data FOSSILS
78 *Transformed variables X'=(X-A)/B
79 *VARIABLES: A      B      Term
80 *D1      0      1      1/sqr(2)
81 *D2      0      1      sin(t)
82 *D3      0      1      cos(t)
83 *D4      0      1      sin(2t)
84 *D5      0      1      cos(2t)
85 *D6      0      1      sin(3t)
86 *D7      0      1      cos(3t)
87 *D8      0      1      sin(4t)
88 *END of plotting specifications
89 *
90 *
91 *
92 *
93 *
94 *

```

```

■ 13 1 SURVO 84 EDITOR 08-13-1984 20:20:05      A: 100 72 32957 0
Andrews' function plots of FOSSILS

```



Data files are created by a FILE CREATE scheme and the data values are saved and edited by the FILE EDIT operation.

The fields can have long names (8 first characters are used as a reference) and the name may include technical information like the output format and the numerical range.

FILE EDIT automatically generates a format for data input according to the structure of the data file.

```
■ 16 1 SURVO 84 EDITOR 08-11-1984 15:35:53          D: 100 100 29600 0
1 *
2 *
3 *FILE CREATE WORLD,1,30,64
4 * Source: Selected Demographic Indicators by Country, 1950-2000:
5 * Demographic estimates and projections as assessed in 1978
6 * United Nations, New York 1980
7 * Projections and estimates for 1985 (medium variant)
8 *
9 *FIELDS:
10 * 1 S 26 Country Name of the country
11 * 2 N 1 Page Page number in the source (####) {16,198}
12 * 3 S 8 Area Major area
13 * 4 S 8 Region
14 * 5 N 4 Popul Population, total in 1000 (#####) {1,1010000}
15 * 6 N 4 Males Population, males in 1000 (#####) {1,520000}
16 * 7 N 4 Ages4 Pop. ages 0-4 to total % (##.##) {5,30}
17 * 8 N 4 Ages14 Pop. ages 5-14 to total % (##.##) {10,40}
18 * 9 N 4 Ages64 Pop. ages 15-64 to total % (##.##) {40,75}
19 * 10 N 4 Old Pop. ages 65+ to total % (##.##) {2,20}
20 * 11 N 4 Med.age Median age (years) (##.##) {14,40}
21 *END
22 *
23 *FILE EDIT WORLD
```

```
14 1 SURVO 84 EDITOR 08-11-1984 15:45:45          100 100 27351
DATA FILE: WORLD      Record # 1          N= 0
Country <Finland>      ▶
Page   <164> Area    <Europe> ▶ Region <Northern> ▶
Popul  44907        ▶ Males   42374      ▶
Ages4  46.8         ▶ Ages14  413.0      ▶
Ages64 468.3        - Old     4           ▶
Med.age 4            ▶
```

More fields in the data file are defined by the FILE UPDATE scheme which has the same structure as FILE CREATE. Also the file and field descriptions may be edited by the FILE UPDATE scheme.

The active fields for subsequent operations with the data file are selected from a display which gives one line for each field.

The active fields are indicated here by 'A's.

The activation process is started and terminated by control-Z.

```
# 18 1 SURVO 84 EDITOR 08-12-1984 13:17:26 D: 100 100 30088 0
1 *
2 *
3 *
4 *FILE UPDATE WORLD
5 * Source: Selected Demographic Indicators by Country, 1950-2000:
6 * Demographic estimates and projections as assessed in 1978
7 * United Nations, New York 1980
8 * Projections and estimates for 1985 (medium variant)
9 *
10 *FIELDS:
11 * 12 N 4 Urban Proportion of urban population % (##.##) {0,99.9}
12 * 13 N 2 Density Population density (per sqr.km.) (#####) {1,5100}
13 * 14 N 4 Growth Rate of growth % (##.##) {-0.3,5}
14 * 15 N 4 Age_mal Life expectancy, males (years) (##.##) {40,80}
15 * 16 N 4 Age_fem Life expectancy, females (years) (##.##) {40,80}
16 *END
17 *
18 *
19 *
20 *
21 *
22 *
23 *
```

---

Data file: WORLD M1= 30 M= 16 N= 150 REC/OBS= 1

N(active fields)= 5 , N(protected fields)= 0

1 -- Country	Name of the country	S 26
2 -- Page	Page number in the source (###) {16,198}	N 1
3 -- Area	Major area	S 8
4 -- Region		S 8
5 -- Popul	Population, total in 1000 (#####) {1,1010000}	N 4
6 -- Males	Population, males in 1000 (#####) {1,520000}	N 4
7 -- Ages4	Pop. ages 0-4 to total % (##.##) {5,30}	N 4
8 -- Ages14	Pop. ages 5-14 to total % (##.##) {10,40}	N 4
9 -- Ages64	Pop. ages 15-64 to total % (##.##) {40,75}	N 4
10 -- Old	Pop. ages 65- to total % (##.##) {2,20}	N 4
11 -- Med.age	Median age (years) (##.##) {14,40}	N 4
12 A- Urban	Proportion of urban population % (##.##) {0,99.9}	N 4
13 A- Density	Population density (per sqr.km.) (#####) {1,5100}	N 2
14 A- Growth	Rate of growth % (##.##) {-0.3,5}	N 4
15 A- Age_mal	Life expectancy, males (years) (##.##) {40,80}	N 4
16 A- Age_fem	Life expectancy, females (years) (##.##) {40,80}	N 4

Indicate active (A,X,Y etc.) and passive (-) fields!

To protection column, press ↵

To stop, press F8:EXIT or ctrl-Z

Usually FILE UPDATE is preceded by a FILE STATUS operation which displays the current structure of the file in the edit field in the same form. This set-up works as a basis for creating new files with a similar structure or for updating the current one.

Now FILE EDIT has been activated again and the user may enter values for the active fields.

```
■ 16 1 SURVO 84 EDITOR 08-12-1984 13:34:03 D: 100 100 30052 0
1 *
2 *
3 *
4 *FILE UPDATE WORLD
5 * Source: Selected Demographic Indicators by Country, 1950-2000:
6 * Demographic estimates and projections as assessed in 1978
7 * United Nations, New York 1980
8 * Projections and estimates for 1985 (medium variant)
9 *
10 *FIELDS:
11 * 12 N 4 Urban Proportion of urban population % (0..99.9)
12 * 13 N 2 Density Population density (per sqr.km.) (0..5100)
13 * 14 N 4 Growth Rate of growth % (-0..3.5)
14 * 15 N 4 Age_mal Life expectancy, males (years) (40..80)
15 * 16 N 4 Age_fem Life expectancy, females (years) (40..80)
16 *END
17 *
18 *
19 *FILE EDIT WORLD
20 *
21 *
22 *
23 *
```

10 1 SURVO 84 EDITOR 08-12-1984 13:42:13	100 100 27550
DATA FILE: WORLD Record # 1 Finland	N= 150
Urban 466.9 ► Density 415 ► Growth 4.3	►
Age_mal 469.3 ► Age_fem 4 ►	

FILE EDIT can also be used for various searches in the current data file. When the cursor is located in a certain field and the SRCH key is pressed, a prompt for starting a search for a specific value of this field is displayed. Here two searches (one for 'Country' and another for 'Growth') are shown.

10 1 SURVO 84 EDITOR 08-11-1984 16:04:39			100	100	22534
DATA FILE: WORLD	Record # 102	Paraguay		N= 150	
Country <Paraguay		>			
Page <101> Area	<America	> Region <Tr.South>			
Popul <3546	> Males <1774	>			
Ages4 <16.7	> Ages14 <26.9	>			
Ages64 <52.9	> Old <3.5	>			
Med.age <18	> Urban <41.5	> Density <9	>		
Growth <2.81	> Age_mal <64.9	>			
Age_fem <68.6	>				

Record to be found ( number or =,<,> Country )? Paraguay

102

To stop, press F8:EXIT

10 1 SURVO 84 EDITOR 08-11-1984 16:16:29			100	100	25638
DATA FILE: WORLD	Record # 31	Kenya		N= 150	
Country <Kenya		>			
Page <19 > Area	<Africa	> Region <Eastern >			
Popul <19864	> Males <9881	>			
Ages4 <20.4	> Ages14 <29.7	>			
Ages64 <47.5	> Old <2.5	>			
Med.age <15	> Urban <16.7	> Density <34	>		
Growth <3.72	> Age_mal <58.6	>			
Age_fem <62.3	>				

Record to be found ( number or =,<,> Growth )? >3

31

To stop, press F8:EXIT

Variables in the data file are transformed and new variables defined by a VAR operation.  
 The data file can be sorted according to any set of variables by the FILE SORT operation.  
 The active fields are displayed in the edit field by the FILE LOAD operation.  
 Thus more extensive searches in data files can be conducted by a sequence of commands and operations.

```
# 22 1 SURVO 84 EDITOR 08-11-1984 17:05:00 A: 100 100 28869 0
1 *
2 *Where females have the greatest life expectancy
3 *when compared with males?
4 *
5 *Original variables in file WORLD:
6 * 15 N 4 Age_mal Life expectancy, males (years) (##.##) {40,80}
7 * 16 N 4 Age_fem Life expectancy, females (years) (##.##) {40,80}
8 *
9 *VAR Ageratio=Age_fem/Age_mal TO WORLD
10 *FILE SORT WORLD BY -Ageratio TO WORLD2
11 *
12 *FILE LOAD WORLD2,1,10
13 *
14 *
15 *
16 *
17 *
18 *
19 *
20 *
21 *
22 *
23 *
```

```
# 22 1 SURVO 84 EDITOR 08-11-1984 17:13:54 D: 100 100 29538 0
1 *
2 *Where females have the greatest life expectancy
3 *when compared with males?
4 *
5 *Original variables in file WORLD:
6 * 15 N 4 Age_mal Life expectancy, males (years) (##.##) {40,80}
7 * 16 N 4 Age_fem Life expectancy, females (years) (##.##) {40,80}
8 *
9 *VAR Ageratio=Age_fem/Age_mal TO WORLD
10 *FILE SORT WORLD BY -Ageratio TO WORLD2
11 *
12 *FILE LOAD WORLD2,1,10
13 *DATA WORLD2*,16,25,14
14 #Country Ageratio
15 *
16 *USSR 1.1394
17 *Finland 1.1183
18 *USA 1.1165
19 *Czechoslovakia 1.1066
20 *Luxemburg 1.1034
21 *Poland 1.1032
22 *Chile 1.1031
23 *France 1.1020
```

FILE STATUS displays the active fields of the data file in the edit field and thus gives general information. It also provides a natural basis for FILE UPDATE and FILE CREATE.

A three-dimensional contingency table is formed by a TAB operation. A classification can be defined for both string fields and numerical variables.

Multidimensional tables are displayed in the natural nested form.

```

■ 14 1 SURVO 84 EDITOR 08-11-1984 10:37:26 D: 100 100 29064 0
1 *SAVE TABLE
2 *
3 *FILE STATUS WORLD2
4 * Source: Selected Demographic Indicators by Country, 1950-2000:
5 * Demographic estimates and projections as assessed in 1978
6 * United Nations, New York 1980
7 * Projections and estimates for 1985 (medium variant)
8 *
9 *FIELDS: (active)
10 * 3 S 8 Area Major area
11 * 11 N 4 Med.age Median age (years) (##.##)
12 * 14 N 4 Growth Rate of growth % (##.##)
13 *END
14 *
15 *TAB WORLD2,21
16 *VARIABLES=Area,Med.age,Growth
17 *Area=/Europe,/Asia,/America,/-{other}
18 *Med.age=0,25(Low),30(Medium),40(High)
19 *Growth=-0.5,1,2,5
20 *
21 *
22 *
23 *

```

```

■ 14 1 SURVO 84 EDITOR 08-11-1984 10:45:11 D: 100 100 29670 0
11 * 11 N 4 Med.age Median age (years) (##.##)
12 * 14 N 4 Growth Rate of growth % (##.##)
13 *END
14 *
15 *TAB WORLD2,21
16 *VARIABLES=Area,Med.age,Growth
17 *Area=/Europe,/Asia,/America,/-{other}
18 *Med.age=0,25(Low),30(Medium),40(High)
19 *Growth=-0.5,1,2,5
20 *
21 *TABLE WORLD21,22,32,F N=150
22 * Area /Europe /Asia /America other
23 *Med.age Growth *****
24 *Low 1 0 0 0 4
25 * 2 1 3 2 11
26 * 5 0 26 15 47
27 *Medium 1 3 1 1 1
28 * 2 0 3 1 3
29 * 5 0 0 0 0
30 *High 1 23 1 1 1
31 * 2 0 0 1 1
32 * 5 0 0 0 0
33 *

```

After a slight modification in the TAB scheme (see the colon in the VARIABLES=Area:Med.age,Growth specification) the same scheme gives several two-dimensional tables with 'Area' as a common background variable.

```

a 14 1 SURVO 84 EDITOR 08-11-1984 10:57:30 D: 100 100 29628 0
1 *SAVE TABLE
2 *
3 *FILE STATUS WORLD2
4 * Source: Selected Demographic Indicators by Country, 1950-2000:
5 * Demographic estimates and projections as assessed in 1978
6 * United Nations, New York 1980
7 * Projections and estimates for 1985 (medium variant)
8 *
9 *FIELDS: (active)
10 * 3 S 8 Area Major area
11 * 11 N 4 Med.age Median age (years) (##.##)
12 * 14 N 4 Growth Rate of growth % (##.##)
13 *END
14 *
15 *TAB WORLD2,21
16 *VARIABLES=Area:Med.age,Growth
17 *Area=/Europe,/Asia,/America,/-<(other)>
18 *Med.age=0,25(Low),30(Medium),40(High)
19 *Growth=-0.5,1,2,5
20 *
21 *
22 *
23 *

```

```

a 14 1 SURVO 84 EDITOR 08-11-1984 11:06:14 D: 100 100 29651 0
11 * 11 N 4 Med.age Median age (years) (##.##)
12 * 14 N 4 Growth Rate of growth % (##.##)
13 *END
14 *
15 *TAB WORLD2,21
16 *VARIABLES=Area:Med.age,Growth
17 *Area=/Europe,/Asia,/America,/-<(other)>
18 *Med.age=0,25(Low),30(Medium),40(High)
19 *Growth=-0.5,1,2,5
20 *
21 *TABLE WORLD21,22,26,F N=150
22 * Area /Europe /Asia /America other
23 *Med.age *****
24 *Low 1 29 17 62
25 *Medium 3 4 2 4
26 *High 23 1 2 2
27 *
28 *TABLE WORLD22,29,33,F N=150
29 * Area /Europe /Asia /America other
30 *Growth *****
31 *1 26 2 2 6
32 *2 1 6 4 15
33 *5 0 26 15 47

```

The CELL=Growth,##.### specification implies the means and standard deviations of 'Growth' to be computed in classes defined by the other specifications. The results are displayed according to the format given in CELL.

---

```

■ 14 1 SURVO 84 EDITOR 08-11-1984 11:17:18 D: 100 100 29622 0
1 *SAVE TABLE
2 *
3 *FILE STATUS WORLD2
4 * Source: Selected Demographic Indicators by Country, 1950-2000:
5 * Demographic estimates and projections as assessed in 1978
6 * United Nations, New York 1980
7 * Projections and estimates for 1985 (medium variant)
8 *
9 *FIELDS: (active)
10 * 3 S 8 Area Major area
11 * 11 N 4 Med.age Median age (years) (##.##)
12 * 14 N 4 Growth Rate of growth % (##.##)
13 *END
14 *
15 *TAB WORLD2,21
16 *VARIABLES=Area,Med.age
17 *Area=/Europe,/Asia,/America,-(other)
18 *Med.age=0,25(Low),30(Medium),40(High)
19 *CELL=Growth,##.###
20 *
21 *
22 *
23 *

```

---

```

■ 14 1 SURVO 84 EDITOR 08-11-1984 11:30:17 D: 100 100 29652 0
11 * 11 N 4 Med.age Median age (years) (##.##)
12 * 14 N 4 Growth Rate of growth % (##.##)
13 *END
14 *
15 *TAB WORLD2,21
16 *VARIABLES=Area,Med.age
17 *Area=/Europe,/Asia,/America,-(other)
18 *Med.age=0,25(Low),30(Medium),40(High)
19 *CELL=Growth,##.###
20 *
21 *TABLE WORLD21,22,32,FMS N=150 Mean and SD of Growth
22 * Area /Europe /Asia /America other
23 *Med.age *****
24 *Low 1 29 17 62
25 * Mean 1.930 2.551 2.685 2.472
26 * SD - 0.576 0.522 0.761
27 *Medium 3 4 2 4
28 * Mean 0.897 1.185 0.935 1.138
29 * SD 0.101 0.474 0.134 0.231
30 *High 23 1 2 2
31 * Mean 0.334 0.500 0.955 0.950
32 * SD 0.285 - 0.092 0.141
33 *

```

Variables for a regression model are selected by activating them with specific labels. For example, the regressand is indicated by 'Y', the regressors by 'X' and the residual by 'R'. The whole set-up may be compressed in the edit field in a MASK specification. Whenever a MASK line is activated, the selection of variables with complete descriptions will be seen temporarily. LINREG DECA,7 computes the regression model defined by MASK and gives the results from line 7 onwards in the edit field.

Data file: DECA M1= 30 M= 15 N= 48 REC/OBS= 1

N(active fields)= 7 , N(protected fields)= 0

1 -- Name	Name of athlete	S	8
2 Y- Points	Total score	(NNNN) {7000,9000}	N 2
3 X- 100m	100 meters run	(NNNN) {500,1200}	N 2
4 X- L_jump	Long jump	(NNNN) {500,1200}	N 2
5 X- Shot_put		(NNNN) {500,1200}	N 2
6 X- Hi_jump	High jump	(NNNN) {500,1200}	N 2
7 X- 400m	100 meters run	(NNNN) {500,1200}	N 2
8 -- Hurdles	110 meters hurdles	(NNNN) {500,1200}	N 2
9 -- Discus		(NNNN) {500,1200}	N 2
10 -- Pole_vlt	Pole vault	(NNNN) {500,1200}	N 2
11 -- Javelin		(NNNN) {500,1200}	N 2
12 -- 1500m	1500 meters run	(NNNN) {400,1200}	N 2
13 -- Height	in centimeters	(NNN) {160,210}	N 2
14 -- Weight	in kilograms	(NNN) {50,120}	N 2
15 R- RES			N 8

Indicate active (A,X,Y etc.) and passive (-) fields!

To protection column, press →

To stop, press F8:EXIT or ctrl-Z

```

■ 14 1 SURVO 84 EDITOR 08-11-1984 17:55:21 D: 100 100 30128 0
1 *
2 *
3 *MASK=-YXXXXX-----R
4 *LINREG DECA,7
5 *
6 *
7 *Linear regression analysis: Data DECA, Regressand Points N=48
8 *Variable Regr.coeff. Std.dev. t beta
9 *100m .5425684 .3063601 1.77 0.199
10 *L_jump 1.361467 .3024766 4.50 0.427
11 *Shot_put 1.17146 .2589412 4.52 0.448
12 *Hi_jump .9223284 .2616502 3.53 0.370
13 *400m 1.327236 .3632046 3.65 0.409
14 *constant 3559.491
15 *Variance of regressand Points = 26132 DF=47
16 *Residual variance=10607.98 DF=42
17 *R=0.79828 R2=0.63725
18 *
19 *
20 *
21 *
22 *
23 *
```

The CORR operation computes the means, standard deviations and correlations for all active fields pointed out by the MASK specification. If MASK is not given, all active fields selected previously (by FIELD ACTIVATE for example) are used. The results are also saved (without rounding) in a special file SURVO.COR on the current data disk. This file may be renamed, if necessary, and used as a starting point for regression and principal components analysis, for example.

```
# 13 1 SURVO 84 EDITOR 08-11-1984 18:07:05 D: 100 100 29603 7
1 *
2 *
3 *MASK=-XXXXXX-----R
4 *LINREG DECA,7
5 *
6 *
7 *Linear regression analysis: Data DECA, Regressand Points N=48
8 *Variable Regr.coeff. Std.dev. t beta
9 *100m .5425684 .3063601 1.77 0.199
10 *L_jump 1.361467 .3024766 4.50 0.427
11 *Shot_put 1.17146 .2589412 4.52 0.448
12 *Hi_jump .9223284 .2616502 3.53 0.370
13 *400m 1.327236 .3632046 3.65 0.409
14 *constant 3559.491
15 *Variance of regressand Points = 26132 DF=47
16 *Residual variance=10607.98 DF=42
17 *R=0.79828 R2=0.63725
18 *
19 *CORR DECA,20
20 *
21 *
22 *
23 *
```

```
# 13 1 SURVO 84 EDITOR 08-11-1984 18:15:14 D: 100 100 29651 0
18 *
19 *CORR DECA,20
20 *Means, std.devs and correlations of DECA N= 48
21 *Variable Mean Std.dev.
22 *Points 7843.47917 161.65395
23 *100m 828.18750 59.30256
24 *L_jump 840.18750 50.72859
25 *Shot_put 740.77083 61.82757
26 *Hi_jump 805.85417 64.80511
27 *400m 813.50000 49.80216
28 *RES 0.00000 97.36257
29 *Correlations:
30 * Points 100m L_jump Shot_p Hi_jum 400m RES
31 *Points 1.000 0.294 0.499 0.364 0.221 0.295 0.602
32 *100m 0.294 1.000 0.172 -0.028 -0.412 0.456 0.000
33 *L_jump 0.499 0.172 1.000 -0.034 -0.003 0.133 0.000
34 *Shot_put 0.364 -0.028 -0.034 1.000 0.163 -0.304 0.000
35 *Hi_jump 0.221 -0.412 -0.003 0.163 1.000 -0.339 0.000
36 *400m 0.295 0.456 0.133 -0.304 -0.339 1.000 0.000
37 *RES 0.602 0.000 0.000 0.000 0.000 0.000 1.000
38 *
39 *
40 *
```

These two exhibits tell a story of making principal components and factor rotation.

First correlations are computed (CORR). Then four (#COMP=4) principal components are extracted (PCOMP).

Finally an interactive and iterative rotation procedure is started by a ROTATE command.

The user can control rotation step by step and consult some analytic criteria when selecting proper rotation angles.

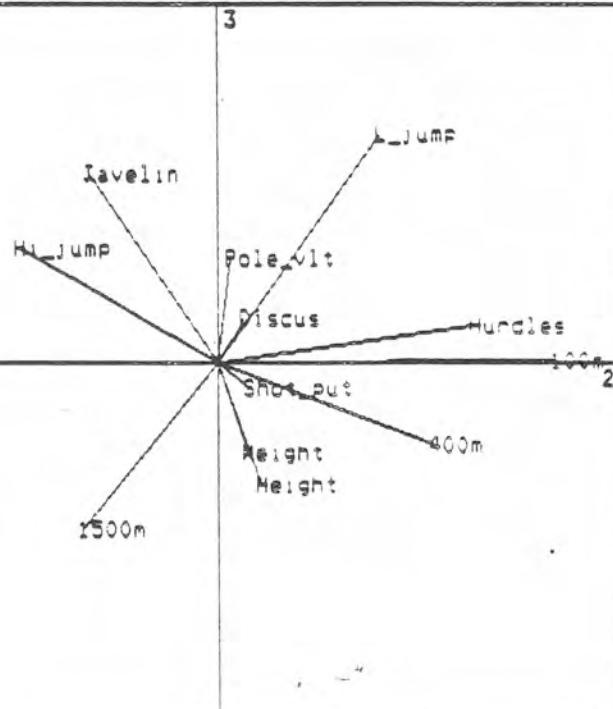
```
# 19 1 SURVO 84 EDITOR 08-20-1984 16:40:45 A: 100 100 28581 0
1 *
2 *MASK=--AAAAAAA / Selecting variables
3 *CORR DECA / Means, std.devs and correlations, results in SURVO.COR
4 #NCOMP=4
5 *PCOMP DECA;SURVO.PCO / Principal components from DECA with SURVO.COR
6 * Results also in file SURVO.PCO
7 *Principal components: Data DECA
8 *      1   2   3   4
9 *100m   -0.128  0.836  0.008 -0.158
10 *L_jump  -0.010  0.405  0.642  0.304
11 *Shot_put  0.843  0.077 -0.067 -0.117
12 *Hi_jump  0.336 -0.485  0.320  0.142
13 *400m    -0.478  0.537 -0.230  0.337
14 *Hurdles  0.153  0.639  0.103  0.249
15 *Discus   0.847  0.068  0.128 -0.136
16 *Pole_vlt -0.355  0.030  0.295 -0.681
17 *Javelin  0.087 -0.315  0.529  0.453
18 *1500m   -0.590 -0.334 -0.467  0.311
19 *Height   0.808  0.109 -0.338  0.199
20 *Weight   0.883  0.074 -0.251  0.016
21 *Eigenval. 3.723  2.035  1.361  1.152
22 *
23 *ROTATE SURVO / Rotating SURVO.PCO
```

#### SURVO 84: FACTOR ROTATION SURVO

Item select: SPACE BAR  
BACKSPACE  
or Initials

Angle of rotation  
Rotate  
Next pair of axes  
Varimax  
Quartimax  
Factor matrix  
Printout (on LPT)  
Exit

Indicate direction of X axis  
by + and - keys!



Computing a linear trend for the mean temperature for 135 consecutive years.

Before the regression analysis a new variable (Trend) is defined by the FILE UPDATE scheme.

The MASK=XY-P indicates the variables (XY) to be selected in the regression model and the variable (P) for the predicted values (Trend). This trend will be employed in the next example.

```
■ 19 1 SURVO 84 EDITOR 08-13-1984 16:31:38 D: 100 100 27662 0
1 *SAVE HEL2
2 *
3 *FILE UPDATE HELSINKI
4 * Mean temperature (C) and rainfall (mm)
5 * Helsinki, July 1844-1978
6 *
7 *FIELDS: (active)
8 * 1 S 4 Year
9 * 2 N 4 Temp Mean temperature (C) in July (##.##)
10 * 3 N 1 Rain Rainfall (mm) in July (####)
11 * 4 N 4 Trend Trend of temperature (##.##)
12 *END
13 *
14 *MASK=XY-P
15 *LINREG HELSINKI,16_
16 *
17 *
18 *
19 *
20 *
21 *
22 *
23 *
```

```
■ 19 1 SURVO 84 EDITOR 08-13-1984 16:49:53 D: 100 100 29610 0
1 *SAVE HEL2
2 *
3 *FILE UPDATE HELSINKI
4 * Mean temperature (C) and rainfall (mm)
5 * Helsinki, July 1844-1978
6 *
7 *FIELDS: (active)
8 * 1 S 4 Year
9 * 2 N 4 Temp Mean temperature (C) in July (##.##)
10 * 3 N 1 Rain Rainfall (mm) in July (####)
11 * 4 N 4 Trend Trend of temperature (##.##)
12 *END
13 *
14 *MASK=XY-P
15 *LINREG HELSINKI,16_
16 *Linear regression analysis: Data HELSINKI, Regressand Temp N=135
17 *Variable Regr.coeff. Std.dev. t beta
18 *Year 8.761096E-03 3.568748E-03 2.45 0.208
19 *constant .3049534
20 *Variance of regressand Temp = 2.709079 DF=134
21 *Residual variance=2.611127 DF=133
22 *R=0.20821 R2=0.04335
23 *
```

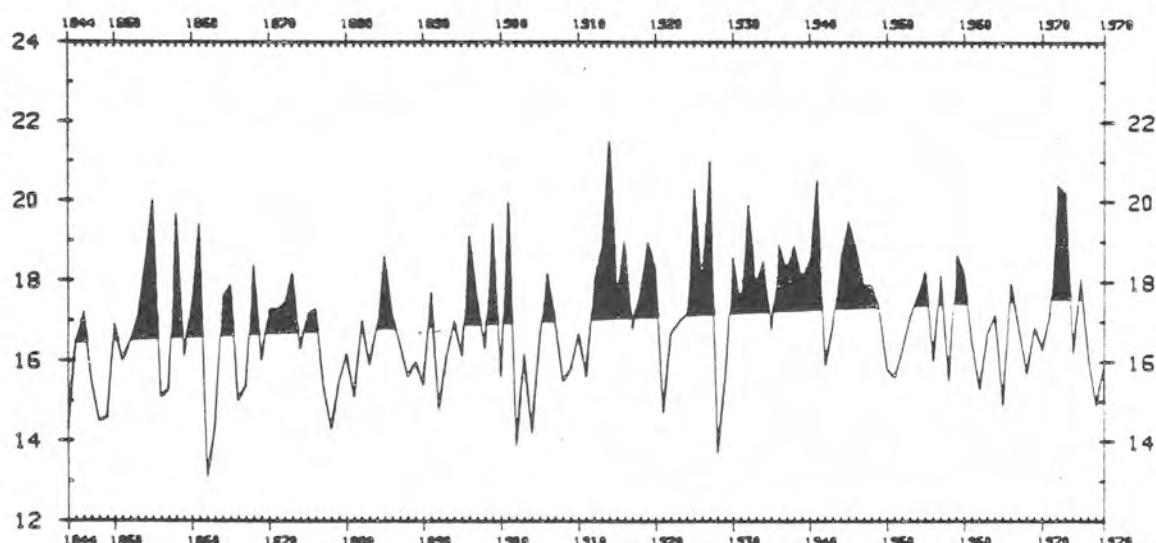
The mean temperature of July in Helsinki is plotted for 135 consecutive years on the SERVOGOR plotter (DEVICE=S). The FILL specifications indicate that the deviations from 'Trend' (computed in the previous example) should shaded using different pens (pen #1 'black' for positive and pen #0 'white' for negative deviations).

```

■ 30 1 SURVO 84 EDITOR 08-20-1984 15:43:58          D: 100 100 29640 0
24 *
25 *
26 *
27 *HEADER=(1,50,50,0,3),HELSINKI:_Mean_temperature_in_July
28 *PLOT HELSINKI,TIME(Year),Temp
29 *XSCALE=(1,20,20,0,1),1,7(10)127,135 TICK=1,1
30 *XSCALE2=(1,20,20,0,1),XSCALE TICK2=1,1
31 *YSCALE=(1,30,30),12(2)24 YSCALE2=(1,30,30),14(2)22
32 *XLABEL= YLABEL= TEXT=(1,20,20,1,1),A A=25_Oct_83/SM,2400,50
33 *DEVICE=S HOME=0,400 SIZE=2650,1500
34 *PEN=1,42,42,0,2 LINE=(1),1 FILL=(1),2,1,135,Trend FILL=(0),1
35 *
36 *
37 *
38 *
39 *
40 *
41 *
42 *
43 *
44 *
45 *
46 *

```

HELSINKI: Mean temperature in July



When several schemes have common specifications, a \*GLOBAL\* subfield in the edit field can be used for them.

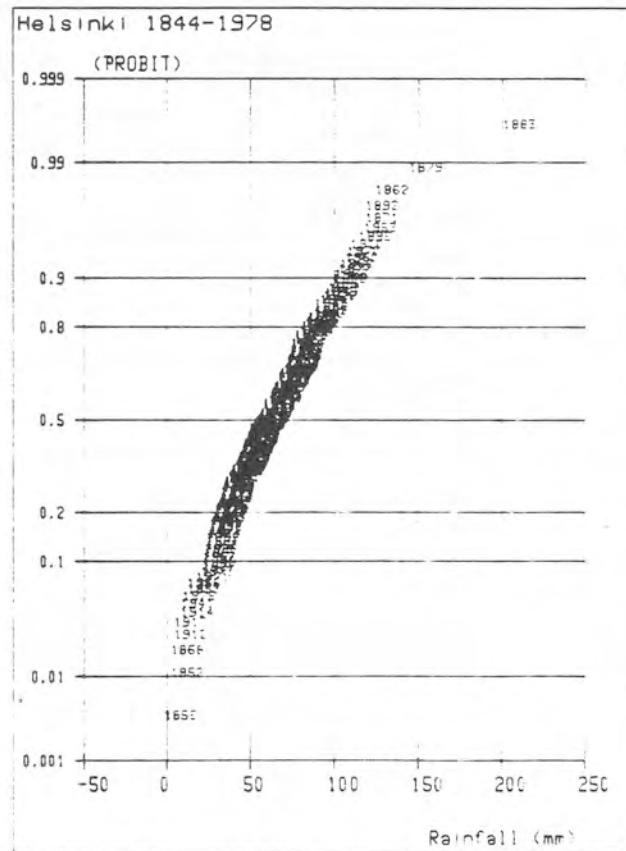
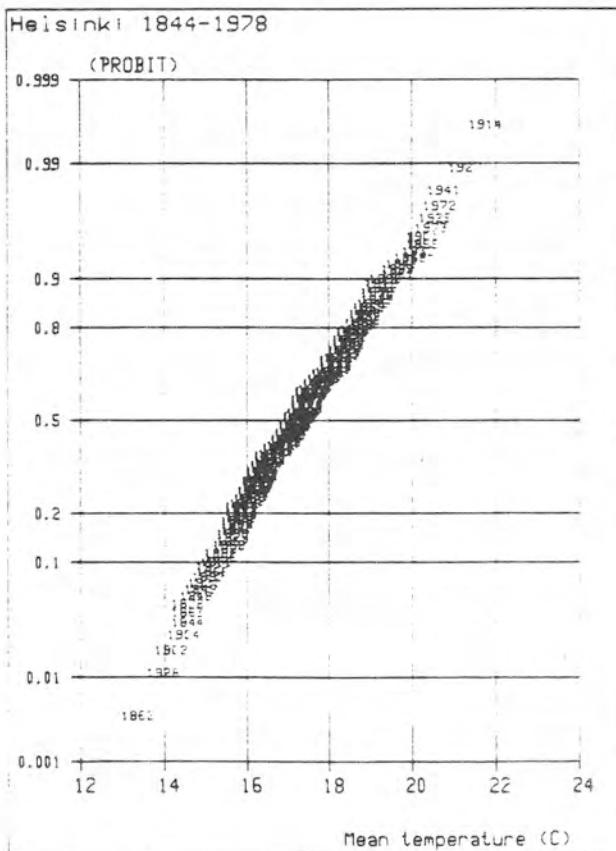
The subfields are separated from each other by dotted border lines (8 and 15 below).

The precedence order of specifications is: local>global>default. The data set HELSINKI is sorted at first with respect to 'TEMP' and then with respect to 'RAIN'. In both cases the ordered sample is plotted on normal probability paper.

```

■ 26 1 SURVO 84 EDITOR 08-14-1984 17:10:31 D: 100 100 29331 0
1 *
2 * *GLOBAL* specifications
3 * DEVICE=S SIZE=1300,1800
4 * GRID=XY TICK=0,1
5 * YSCALE=(1,24,18),PROBIT,0.001,0.01,0.1,0.2,0.5,0.8,0.9,0.99,0.999
6 * HEADER=(2,30,30,0,2),Helsinki_1844-1978
7 * PEN=1,30,24 XDIV=150,1050,100 YDIV=200,1450,150
8 *****
9 *FILE SORT HELSINKI BY Temp TO HELSORT
10 *PLOT HELSORT,Temp,PROBIT
11 *
12 *XSCALE=12(2)24 POINT=(2,18,18),Year
13 *XLABEL=Mean_temperature_(C)
14 *
15 *****
16 *FILE SORT HELSINKI BY Rain TO HELSORT2
17 *PLOT HELSORT2,Rain,PROBIT
18 *
19 *HOME=1350,0
20 *XSCALE=-50(50)250 POINT=(2,18,18),Year
21 *XLABEL=Rainfall_(mm)
22 *
23 *

```



HISTO is a SURVO 84 operation for making of histograms and for fitting of univariate statistical distributions to the data. In this example the mean temperature and the rainfall of Helsinki in July are studied for 135 consecutive years. Both variables are fitted by a normal distribution. By using proper HOME and SIZE specifications several pictures can be displayed simultaneously. HISTO also performs a goodness-of-fit test (not displayed here). HELSINKI is a SURVO 84 data file on the current data disk.

```
■ 20 1 SURVO 84 EDITOR 07-21-1984 20:10:37 A: 72 72 34105 0
50 *
51 * Mean temperature and rainfall in Helsinki, July 1865-1978
52 *HISTO HELSINKI,Temp
53 *Temp=10(0.50)24 XSCALE=10(5)25 FIT=NORMAL XLABEL=Temperature_(C)
54 *HOME=70,0 SIZE=365,350 XDIV=40,300,25 GRID=XY TICK=0.5,1
55 *oooooooooooooooooooooooooooooooooooooooooooooooooooo
56 *HISTO HELSINKI,Rain
57 *Rain=-50(10)250 XSCALE=-50(50)250 FIT=NORMAL XLABEL=Rainfall_(mm)
58 *HOME=434,0 SIZE=365,350 XDIV=40,300,25 GRID=XY TICK=10,1
59 *
60 *
61 *
62 *
63 *
64 *
65 *
66 *
67 *
68 *
69 *
70 *
71 *
72 *
```

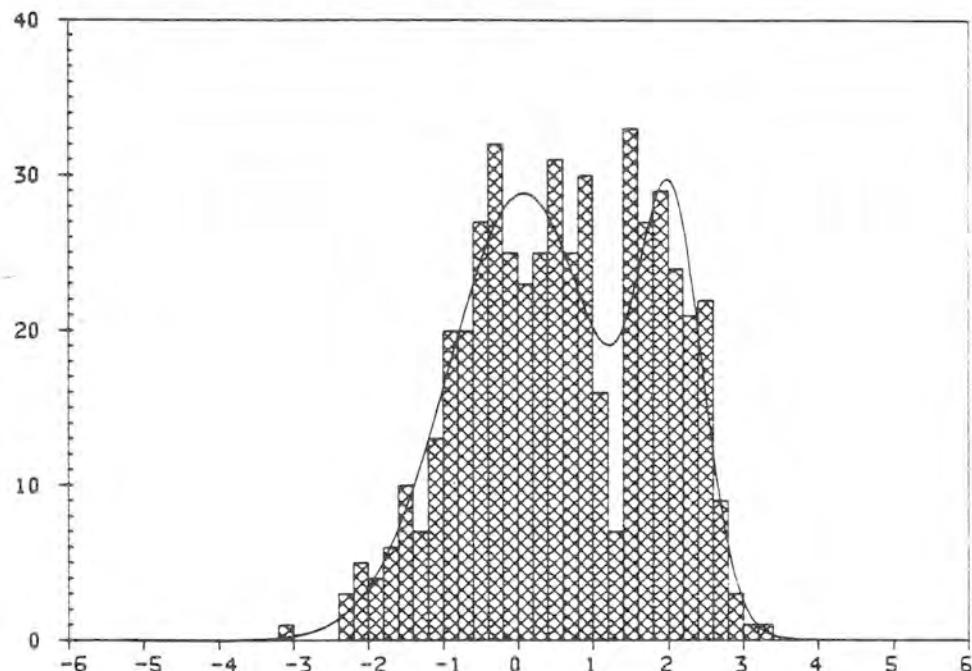
```
■ 20 1 SURVO 84 EDITOR 07-21-1984 20:33:53 A: 72 72 34453 0
50 *
51 * Mean temperature and rainfall in Helsinki, July 1865-1978
52 *HISTO HELSINKI,Temp
53 *Temp=10(0.50)24 XSCALE=10(5)25 FIT=NORMAL XLABEL=Temperature_(C)
54 *HOME=70,0 SIZE=365,350 XDIV=40,300,25 GRID=XY TICK=0.5,1
55 *oooooooooooooooooooooooooooooooooooooooooooooooooooo
56 *HISTO HELSINKI,Rain
57 *Rain=-50(10)250 XSCALE=-50(50)250 FIT=NORMAL XLABEL=Rainfall_(mm)
58 *HOME=434,0 SIZE=365,350 XDIV=40,300,25 GRID=XY TICK=10,1
59 *
60 * Histogram of Temp in HELSINKI Histogram of Rain in HELSINKI
61 * Frequency Frequency
62 * 30 30
63 * 20 20
64 * 10 10
65 * 0 0
66 * 10 10
67 * 20 20
68 * 30 30
69 * 0 0
70 * 10 10
71 * 20 20
72 *
```

Estimating parameters of a mixture of two normal distributions. In this experiment a data file SIMUDATA is created (FILE CREATE) and 500 observations from a certain mixture are generated by a VAR operation.

Finally the parameters are re-estimated by the HISTO operation which also plots the frequency distribution and the fitted density function.

```
# 26 1 SURVO 84 EDITOR 08-20-1984 14:59:45 D: 100 100 27387 0
1 #
2 *FILE CREATE SIMUDATA,1*4,10,64,500
3 * Sample (N=500) from a mixture of two normal distributions
4 *FIELDS:
5 * 1 N 4 Mixnorm
6 *END
7 *****
8 *VAR TO SIMUDATA
9 *BASIC
10 *      W=%Uniform(0,1):IF W<0.7 THEN Popul2!
11 *      Mixnorm=%Normal(2,0.25):GOTO END
12 *Popul2!  Mixnorm=%Normal(0,1)
13 *END
14 *****
15 *HISTO SIMUDATA,Mixnorm,25 / HOME=200,0 SIZE=2400,1800
16 *HEADER=(1,50,40,1,3),Mixture_of_two_normal_distributions
17 *Mixnorm=-6(0.2)6 XSCALE=-6(1)6 YSCALE=0(10)40 TICK=0,1
18 *DEVICE=S PEN=1,30,30,0,2 SHADING=4
19 *FIT=MIXNORM INIT=0.5,2,0.5,0,1 STEP=0.1
20 *
21 *DENSITY MIXNORM(p,m1,s1,m2,s2)
22 *Y=0.39894226*(p/s1*EXP(-0.5*((X-m1)/s1)^2)+(1-p)/s2*EXP(-0.5*((X-m2)/s2)^2)
23 *END
```

*Mixture of two normal distributions*



(Continuation)

Besides the graphical output HISTO displays numerical results in the edit field (if a line label is given in the HISTO operation). The estimated parameters as well as their standard errors and correlations are produced. Furthermore a table of observed and expected frequencies and the  $\chi^2$  statistic is printed.

```

# 1 1 SURVO 84 EDITOR 08-12-1984 21:01:06 D: 100 100 29589 0
24 *
25 *HISTO: Estimated parameters of MIXNORM
26 *p=0.271094 (0.033635)
27 *m1=2.047 (0.054054)
28 *s1=0.428125 (0.039643)
29 *m2=0.076563 (0.086999)
30 *s2=1.008 (0.059888)
31 *Correlations:
32 *      p     m1     s1     m2     s2
33 *p      1.000 -0.457  0.460 -0.645 -0.602
34 *m1    -0.457  1.000 -0.436  0.380  0.265
35 *s1     0.460 -0.436  1.000 -0.381 -0.319
36 *m2    -0.645  0.380 -0.381  1.000  0.608
37 *s2    -0.602  0.265 -0.319  0.608  1.000
38 *LOG(L)=-791.320 NF= 381
39 *Frequency distribution of Mixnorm in SIMUDATA: N=500
40 *                                min e=5
41 *Class midpoint   f    %   Sum   %   e   e   f   X#2
42 * <   -3.1       0   0.0   0   0.0   0.2
43 *      -3.1       1   0.2   1   0.2   0.2
44 *      -2.9       0   0.0   1   0.2   0.4
45 *      -2.7       0   0.0   1   0.2   0.7
46 *      -2.5       0   0.0   1   0.2   1.1

```

```

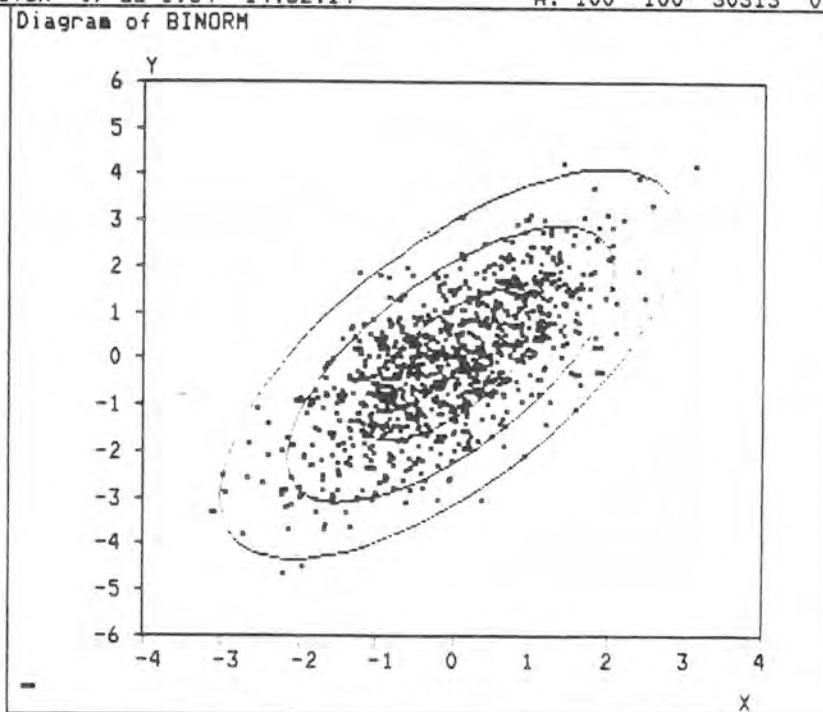
# 1 1 SURVO 84 EDITOR 08-12-1984 21:11:44 D: 100 100 29845 0
58 * -0.1   25  5.0  173  34.6  28.3  28.3  25  0.4
59 *  0.1   23  4.6  196  39.2  28.8  28.8  23  1.2
60 *  0.3   25  5.0  221  44.2  28.1  28.1  25  0.3
61 *  0.5   31  6.2  252  50.4  26.4  26.4  31  0.8
62 *  0.7   25  5.0  277  55.4  24.0  24.0  25  0.0
63 *  0.9   30  6.0  307  61.4  21.4  21.4  30  3.5
64 *  1.1   16  3.2  323  64.6  19.5  19.5  16  0.6
65 *  1.3    7  1.4  330  66.0  19.5  19.5   7  8.0
66 *  1.5   33  6.6  363  72.6  21.9  21.9  33  5.6
67 *  1.7   27  5.4  390  78.0  26.0  26.0  27  0.0
68 *  1.9   29  5.8  419  83.8  29.2  29.2  29  0.0
69 *  2.1   24  4.8  443  88.6  28.6  28.6  24  0.7
70 *  2.3   21  4.2  464  92.8  23.6  23.6  21  0.3
71 *  2.5   .22  4.4  486  97.2  16.1  16.1  22  2.2
72 *  2.7    9  1.8  495  99.0  9.0   9.0   9  0.0
73 *  2.9    3  0.6  498  99.6  4.2
74 *  3.1    1  0.2  499  99.8  1.6
75 *  3.3    1  0.2  500 100.0  0.6
76 * >  3.3    0  0.0  500 100.0  0.3   6.7   5  0.4
77 *Mean=0.611600 Std.dev.=1.248
78 *Fitted by MIXNORM(0.271094,2.047,0.428125,0.076563,1.008) distribution
79 *Chi-square=28.2 df=19 P=0.9211
80 *

```

This example tells, how easily artificial data can be generated and rather complicated experiments performed. The orbits around this galaxy are concentration ellipses on probability levels given by CONTOUR=0.5,0.9,0.99. Since N=1000, the expected number of cases lying outside the largest orbit is 10. Now we have 8 or 9, which is plausible.

```
■ 16 1 SURVO 84 EDITOR 07-22-1984 14:35:58 A: 100 100 29486 0
1 *SAVE BINORM
2 *
3 *Generating a sample of 1000 observations from a two-dimensional
4 *normal distribution:
5 *
6 *Creating data file BINORM:
7 *FILE CREATE BINORM,1*8,2,64,1000
8 *FIELDS:
9 * 1 N 4 X      X is N(0,1)
10 * 2 N 4 Y     Y=X+W, where W is N(0,1)
11 *END
12 *#####
13 *
14 *Generating the sample:
15 *VAR TO BINORM
16 *BASIC
17 *X=%Normal(0,1)
18 *W=%Normal(0,1):Y=X+W
19 *END
20 *#####
21 *
22 *Plotting the bivariate sample:
23 *PLOT BINORM,X,Y / XSCALE=-4(1)4 YSCALE=-6(1)6 CONTOUR=0.5,0.9,0.99
```

```
■ 16 1 SURVO 84 EDITOR 07-22-1984 14:52:14 A: 100 100 30313 0
```



Simple curve plotting without any extra specifications.  
After plotting the edit field may be freely scrolled over the graph.

■ 20 1 SURVO 84 EDITOR 07-22-1984 10:13:58 A: 100 72 32912 0

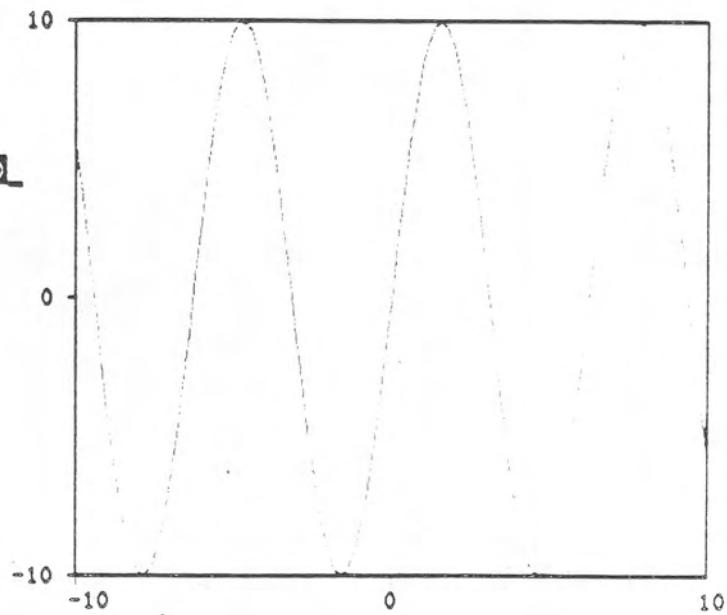
```

1 *
2 *
3 *
4 *
5 *
6 *
7 *
8 *PLOT Y(X)=10*SIN(X)
9 *
10 *
11 *
12 *
13 *
14 *
15 *
16 *
17 *
18 *
19 *
20 *
21 *
22 *
23 *
```

■ 20 1 SURVO 84 EDITOR 07-22-1984 10:21:25 A: 100 72 33076 0

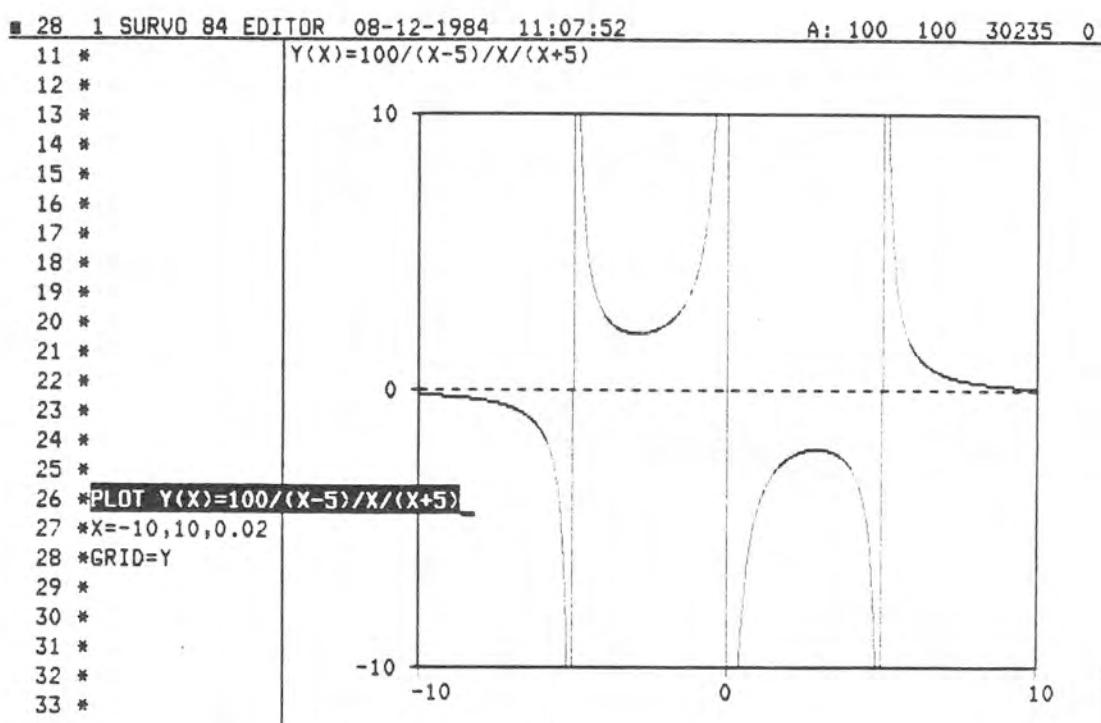
```

1 *
2 *
3 *
4 *
5 *
6 *
7 *
8 *PLOT Y(X)=10*SIN(X)
9 *
10 *
11 *
12 *
13 *
14 *
15 *
16 *
17 *
18 *
19 *
20 *
21 *
22 *
23 *
```



A rational function with 3 points of discontinuity is plotted. Observe that, due to a small step length (0.02), the vertical asymptotes are plotted automatically when jumping from one edge to another.

```
# 28 1 SURVO 84 EDITOR 08-12-1984 10:56:41          A: 100 100 29860 0
11 *
12 *
13 *
14 *
15 *
16 *
17 *
18 *
19 *
20 *
21 *
22 *
23 *
24 *
25 *
26 *PLOT Y(X)=100/(X-5)/X/(X+5)
27 *X=-10,10,0.02
28 *GRID=Y
29 *
30 *
31 *
32 *
33 *
```



A curve family telling about compound interest for various interest rates is plotted.

LOG in the YSCALE specification selects the logarithmic scale which transforms an exponential growth to a linear one.

```
■ 22 1 SURVO 84 EDITOR 07-22-1984 12:24:45 A: 100 72 31822 0
1 *SAVE CURVES
2 *
3 *
4 *
5 *
6 *
7 *
8 *
9 *
10 *
11 *
12 *
13 *
14 *
15 *
16 *
17 *
18 *
19 *
20 *PLOT Y(X)=(1+P/100)*X
21 *HEADER=Compound_interest_for_P=5,6,...,15% XLABEL=Years GRID=XY
22 *XSCALE=0(5)30 YSCALE=LOG,1,2,5,10,20,50,100
23 *P=5,15,1 X=0,30,30 HOME=70,150 SIZE=729,400
```

```
■ 22 1 SURVO 84 EDITOR 07-22-1984 12:32:42 A: 100 72 32943 0
```

```
1 *SAVE CURVES
2 * Compound interest for P=5,6,...,15%
3 *
4 * (LOG)
5 * 100
6 * 50
7 * 20
8 * 10
9 *
10 *
11 *
12 *
13 *
14 *
15 *
16 *
17 *
18 *
19 *
20 *PLOT Y(X)=(1+P/100)*X
21 *HEADER=Compound_interest_for_P=5,6,...,15% XLABEL=Years GRID=XY
22 *XSCALE=0(5)30 YSCALE=LOG,1,2,5,10,20,50,100
23 *P=5,15,1 X=0,30,30 HOME=70,150 SIZE=729,400
```

The cumulative distribution functions of standard normal and t distributions with n=2,3,...,10 degrees of freedom are plotted on normal probability paper. 'PROBIT' in the YSCALE specification selects the probit scale. PLOT INTEGRAL implies that the integral function is to be plotted and INTEGRAL=1 that the function should be scaled so that its integral is 1 in the plotting range.

```
■ 33 1 SURVO 84 EDITOR 08-12-1984 09:37:10 A: 100 100 29602 0
1 *
2 *
3 *
4 *
5 *
6 *
7 *
8 *
9 *
10 *
11 *
12 *
13 *
14 *
15 *
16 *
17 *HEADER=t_distribution_limiting_to_normal_distribution
18 *HOME=100,200 SIZE=500,350
19 *INTEGRAL=1 XSCALE=-5(1)5 YSCALE=PROBIT,0.01,0.1,0.5,0.9,0.99
20 *
21 *PLOT INTEGRAL Y(X)=exp(-0.5*X^2)
22 *PLOT INTEGRAL Y(X)=(1+X^2/n)^(-(n+1)/2) / n=2,10,1
23 *
```

```
■ 40 1 SURVO 84 EDITOR 08-12-1984 09:50:47 A: 100 100 30122 0
1 *
2 *      t distribution limiting to normal distribution
3 *
4 *      (PROBIT)
5 *
6 *
7 *
8 *
9 *
10 *
11 *
12 *
13 *
14 *
15 *
16 *
17 *HEADER=t_distribution_limiting_to_normal_distribution
18 *HOME=100,200 SIZE=500,350
19 *INTEGRAL=1 XSCALE=-5(1)5 YSCALE=PROBIT,0.01,0.1,0.5,0.9,0.99
20 *
21 *PLOT INTEGRAL Y(X)=exp(-0.5*X^2)
22 *PLOT INTEGRAL Y(X)=(1+X^2/n)^(-(n+1)/2) / n=2,10,1
23 *
```

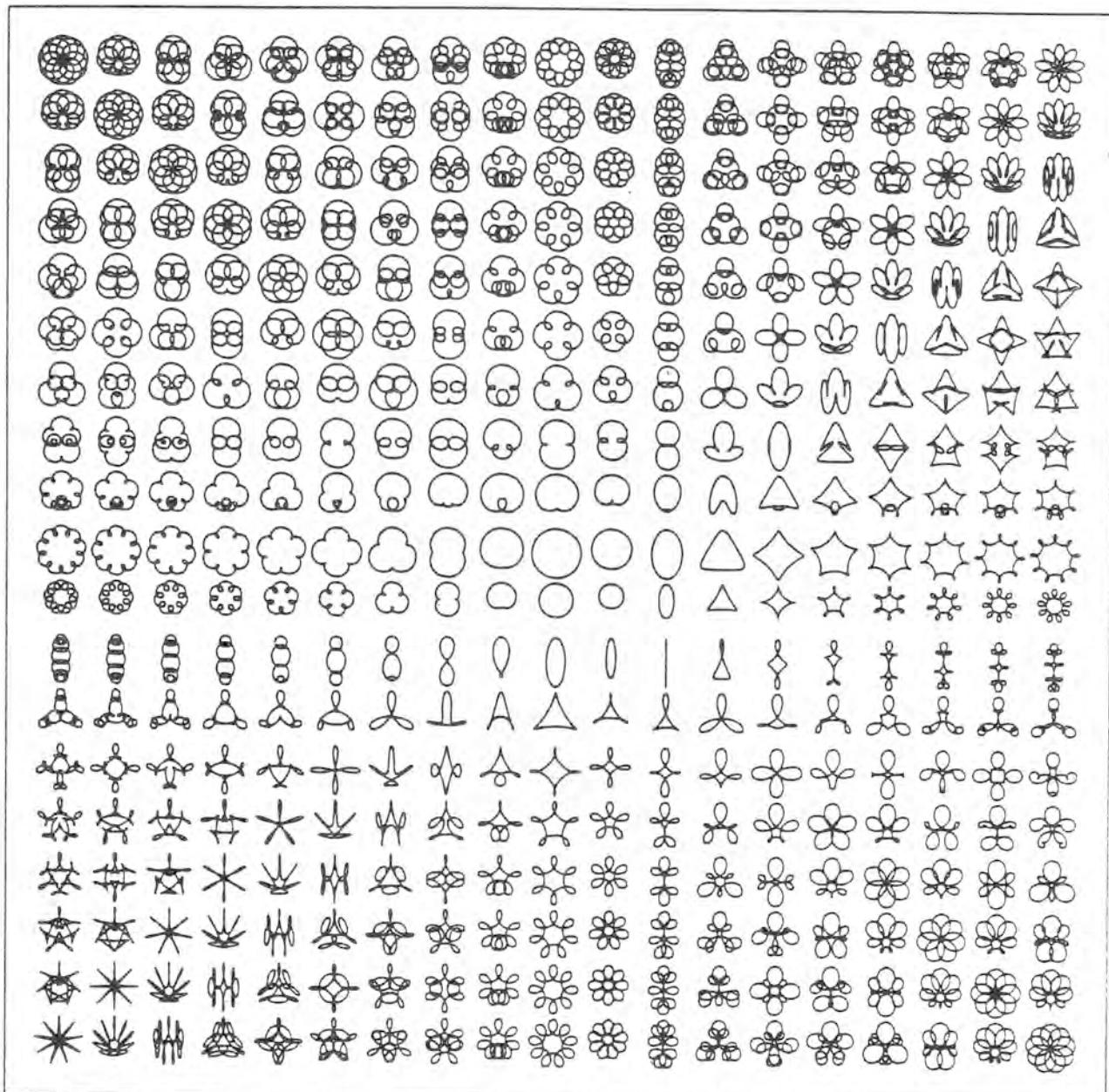
This curve plotting example emphasizes the fact that not so much information is required for producing varied forms and shapes. All information SURVO 84 needs for this picture, can be seen on lines 48-52. A slight modification in parameters would lead to totally different patterns.

```
■ 1 1 SURVO 84 EDITOR 07-22-1984 11:28:14 A: 100 72 32603 0
47 *
48 *HEADER= HOME=200,0 SIZE=450,450
49 *XSCALE=0,4 YSCALE=0,4 XDIV=0,1,0 YDIV=0,1,0
50 *t=0,50,1 r=.1,.5,.1 n=0,8,1 FRAME=0
51 *PLOT X(t)=0.9*r*cos((8*r+n)*t)+int(n/3)+1,
52 *      Y(t)=r*sin((8*r+n)*t)+n+1-3*int(n/3)
53 *
54 *
55 *
56 *
57 *
58 *
59 *
60 *
61 *
62 *
63 *
64 *
65 *
66 *
67 *
68 *
69 *
```

```
■ 1 1 SURVO 84 EDITOR 07-22-1984 11:45:05 A: 100 72 33017 0
47 *
48 *HEADER= HOME=200,0 SIZE=450,450
49 *XSCALE=0,4 YSCALE=0,4 XDIV=0,1,0 YDIV=0,1,0
50 *t=0,50,1 r=.1,.5,.1 n=0,8,1 FRAME=0
51 *PLOT X(t)=0.9*r*cos((8*r+n)*t)+int(n/3)+1,
52 *      Y(t)=r*sin((8*r+n)*t)+n+1-3*int(n/3)
53 *
54 *
55 *
56 *
57 *
58 *
59 *
60 *
61 *
62 *
63 *
64 *
65 *
66 *
67 *
68 *
69 *
```

Another family of curves yielding diverse shapes.  
 All forms in this picture could be interpreted as  
 variations of a simple circle appearing in the middle  
 and thus representing 'the origin of species'.  
 See, how systematically the patterns are developing  
 in different directions.

```
# 56 1 SURVO B4 EDITOR 08-18-1984 20:14:02      A: 100 100 29373 0
1 *
2 *XDIV=0,1,0 YDIV=0,1,0 SIZE=2650,2650 HEADER= FRAME=1
3 *A=-8,10,1      B=-8,10,1      T=0,6.3,0.03
4 *XSCALE=-9,11   YSCALE=-9,11   DEVICE=S
5 *
6 *PLOT X(T)=A+0.225*COS(T)+0.139*COS(A*T)+0.086*COS(B*T),
7 *           Y(T)=B+0.225*SIN(T)+0.139*SIN(A*T)+0.086*SIN(B*T)
8 *
9 *
10 *
```

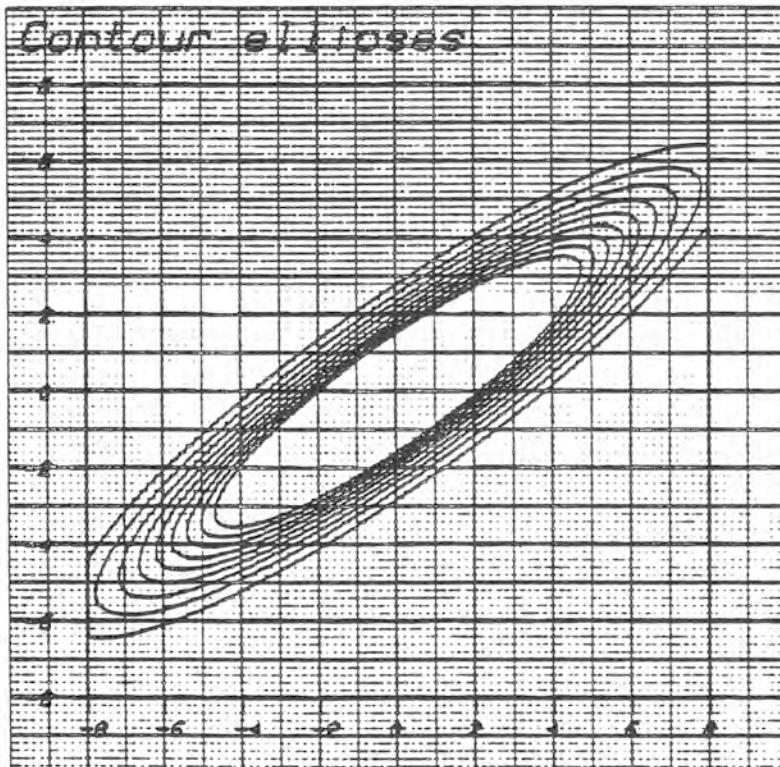


Plotting a graph paper and curves on it.

Firstly a 100 mm x 100 mm grid of parallel lines is drawn by using a single pen with a 0.12 mm tip. The thicker lines are produced in 3 or 5 passes. The series of six PLOT operations does the job automatically.

Then a family of contour ellipses from a two-dimensional normal distribution is plotted. Parameter eps controls the confidence level. (The graph is presented in original scale.)

```
# 40 1 SURVO 84 EDITOR 08-17-1984 18:24:35 A: 100 100 28185 0
1 #
2 *XDIV=0,1,0 YDIV=0,1,0 SIZE=1000,1000
3 *HEADER= FRAME=0 DEVICE=S PEN=2
4 *XSCALE=0,1000 YSCALE=0,1000 HOME=250,50
5 *t10=0,1000,100 t5=50,950,100 t=0,1000,10
6 *eps10=-2,2,1 eps5=-1,1,1 u=0,1000,100
7 #
8 *PLOT Y(u)=t10+eps10           / X lines 10 mm, thickness 5
9 *PLOT Y(u)=t5+eps5            / X lines 5 mm, thickness 3
10 *PLOT Y(u)=t                / X lines 1 mm, thickness 1
11 *PLOT X(u)=t10+eps10,Y(u)=u / Y lines 10 mm, thickness 5
12 *PLOT X(u)=t5+eps5,Y(u)=u / Y lines 5 mm, thickness 3
13 *PLOT X(u)=t,Y(u)=u        / Y lines 1 mm, thickness 1
14 *XXXXXXXXXXXXXXXXXXXXXXXXXXXXXX
15 #
16 *PLOT X(t)=s1*sqr(-2*log(1-eps))*cos(t),
17 *      Y(t)=s2*sqr(-2*log(1-eps))*sin(t+atn(rho/sqr(1-rho*rho)))
18 #
19 *HEADER=(1,36,36,1,2),Contour_ellipses DEVICE=S
20 *s1=4 s2=3 rho=0.9 t=0,6.2832 eps=0.5,0.9,0.05
21 *XDIV=1,8,1 YDIV=1,8,1 SIZE=1000,1000 HOME=250,50 FRAME=1
22 *XSCALE=(1,20,20,1),-8(2)8 YSCALE=(1,20,20,1),-8(2)8
23 #
```



The equations of more complicated curves may be written as 'BASIC' programs in the edit field.  
 Observe that the statement lines may have symbolic labels (like REPEAT!, OLD! etc.).

```

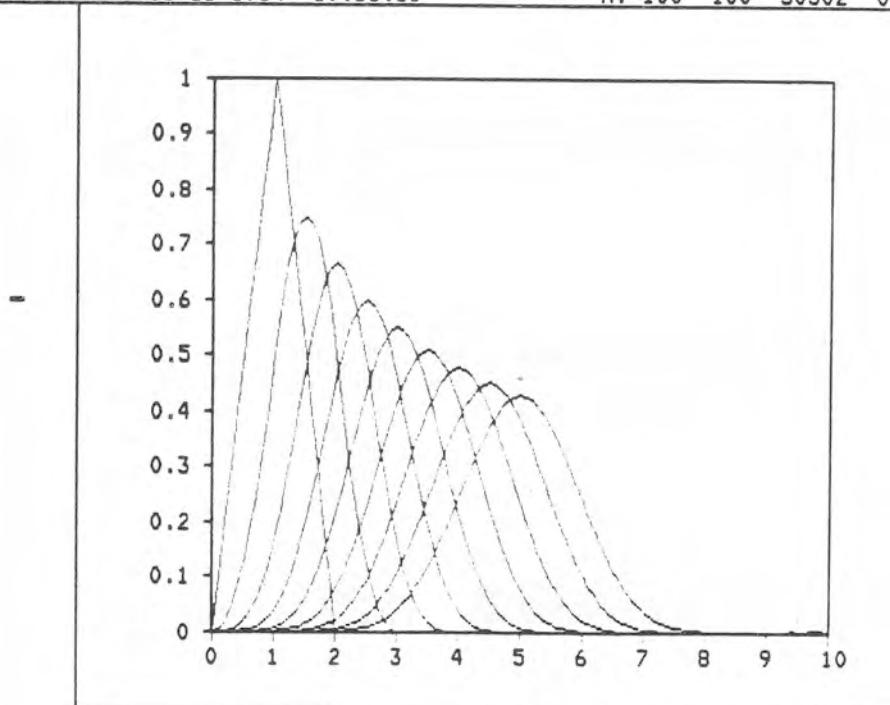
■ 10 1 SURVO 84 EDITOR 08-11-1984 19:41:04 A: 100 100 29372 0
1 *SAVE UNIFORM
2 *
3 *
4 *
5 *
6 *      Plotting the density functions of the sum of n independent
7 *      variables uniformly distributed over (0,1)
8 *
9 *XSCALE=0(1)10 YSCALE=0(0.1)1 n=2,10,1
10 *PLOT F(X)
11 *      IF X>0 THEN OLD! ELSE WFACTORIAL=1:WTERM=1
12 *REPEAT!  WTERM=WTERM+1:IF WTERM>n-1 THEN OLD!
13 *      WFACTORIAL=WFACTORIAL*WTERM:GOTO REPEAT!
14 *OLD!    Y=0:IF X>n THEN READY!
15 *      WCOEFF=1:WIND=0
16 *SUM!    Y=Y+WCOEFF*(X-WIND)^(n-1)
17 *      WIND=WIND+1:IF X<=WIND THEN READY!
18 *      WCOEFF=-(n-WIND+1)/WIND*WCOEFF:GOTO SUM!
19 *READY!  Y=Y/WFACTORIAL
20 *END
21 *
22 *
23 *

```

```

■ 10 1 SURVO 84 EDITOR 08-11-1984 19:51:51 A: 100 100 30302 0

```



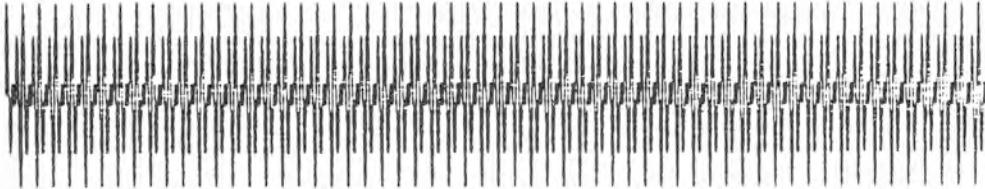
Oscillograms for certain musical intervals are plotted. This kind of a representation clearly reveals the beats which indicate the impureness of the sound as long cycle oscillations. The howling of the extremely dissonant 'Wolf' fifth in the ancient mean tone temperament is striking. To gain more accuracy, these graphs are made on the SERVOGOR plotter (specification DEVICE=S)

```

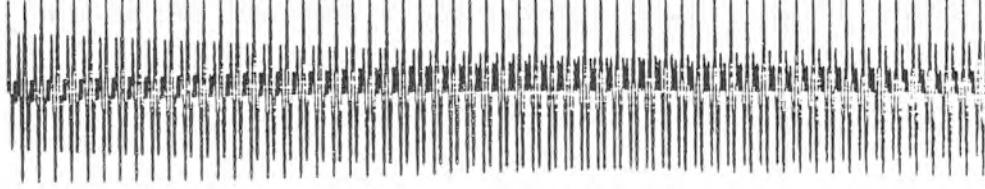
■ 34 1 SURVO 84 EDITOR 07-22-1984 19:54:38      A: 100 100 27319 0
67 *
68 *      Musical intervals in different temperaments
69 *
70 *HEADER=Pure_Fifth
71 *PLOT Y(X)=(SIN(20*X)+SIN(30*X))/2
72 *YSCALE=-1,0,1
73 *XSCALE=0,37.699/12*PI X=0,37.699,0.001
74 *HOME=0,1200 SIZE=2650,600 YDIV=50,500,50 XDIV=100,2500,50
75 *DEVICE=S PEN=1,30,30 FRAME=0
76 *#####
77 *HEADER=Fifth_in_Equal_Temperament          20*2^(7/12)=29.96614
78 *PLOT Y(X)=(SIN(20*X)+SIN(29.96614*X))/2
79 *YSCALE=-1,0,1
80 *XSCALE=0,37.699/12*PI X=0,37.699,0.001
81 *HOME=0,600  SIZE=2650,600 YDIV=50,500,50 XDIV=100,2500,50
82 *DEVICE=S PEN=1,30,30 FRAME=0
83 *#####
84 *HEADER='Wolf'-Fifth_in_Mean_Tone_Temperament 20*128*5^(-11/4)=30.62476
85 *PLOT Y(X)=(SIN(20*X)+SIN(30.62476*X))/2
86 *YSCALE=-1,0,1
87 *XSCALE=0,37.699/12*PI X=0,37.699,0.001
88 *HOME=0,0    SIZE=2650,600 YDIV=50,500,50 XDIV=100,2500,50
89 *DEVICE=S PEN=1,30,30 FRAME=0

```

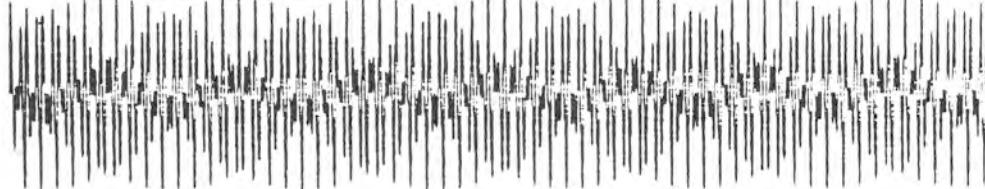
Pure Fifth



Fifth in Equal Temperament



'Wolf'-Fifth in Mean Tone Temperament



Hermann Helmholtz (1821-1894) in his great treatise 'On The Sensations of Tone' has presented a graph on the degree of harmoniousness of consonances. It is based on his theory of physiological acoustics (see pp.192-3 and App.XV).

Here another (and simpler) proposal is introduced. The assumption behind our model is that each (impure) interval  $x$  is conceived as a simple ratio  $n/m$ . The ear likes to keep  $n$  and the beat  $(mx-n)/n$  as small as possible simultaneously.

The balance between these two conflicting factors is controlled by parameter  $c$  which represents the sensitivity of the ear.

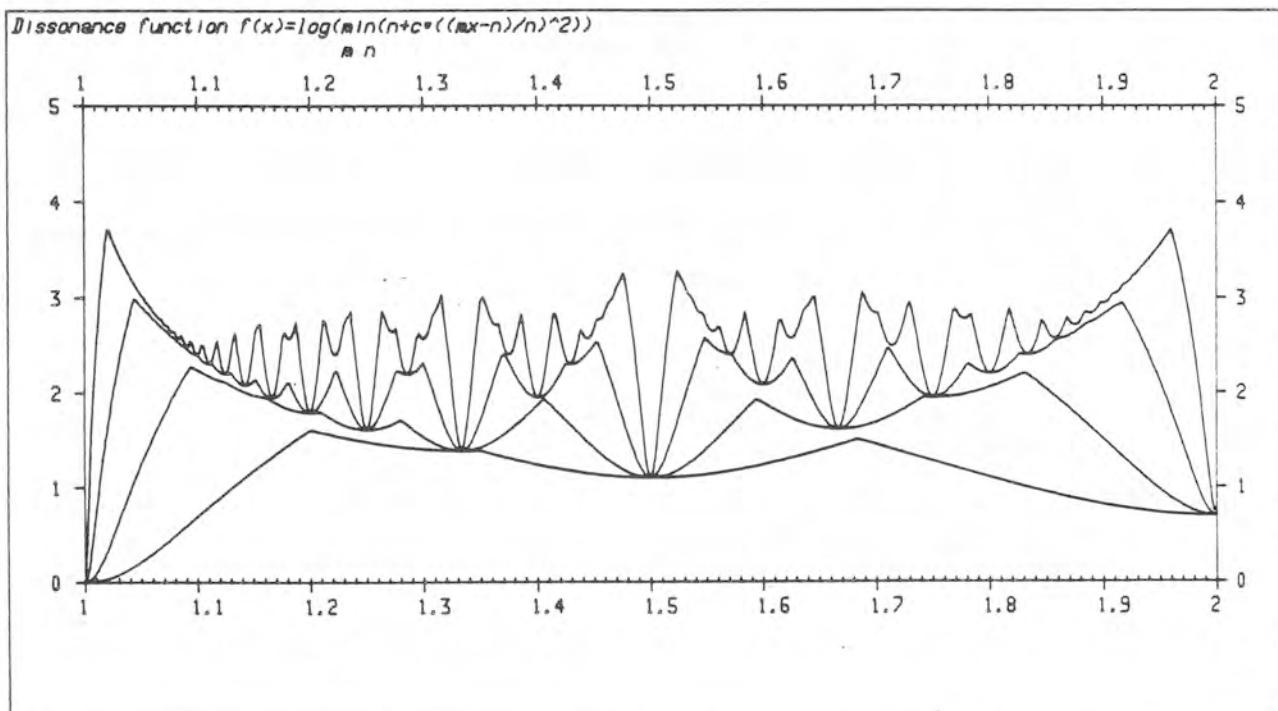
The dissonance curve has been plotted for 4 different ears.

Observe that the PLOT scheme finds the minimum with respect to  $n$  for each  $x$  separately before moving the pen.

```

■ 10 1 SURVO 84 EDITOR 08-20-1984 16:32:24      A: 100 100 29445 0
1 *
2 *
3 *Degree of dissonance for intervals from Unison to Octave
4 *
5 *HEADER=(1,30,24,1),Dissonance_function_f(x)=log(min(n+c*((mx-n)/n)^2))
6 *TEXT=A A=(1,30,24,1),m_n,720,1420
7 *XSCALE=(1,30,24),1(0.1)2 YSCALE=(1,30,24),0(1)5
8 *XSCALE2=(1,30,24),XSCALE YSCALE2=(1,30,24),YSCALE
9 *X=1,2,0.002 TICK=0.01 TICK2=TICK
10 *DEVICE=S SIZE=2690,1500 XDIV=100,1500,90
11 *The sensitivity of the ear: ACCURACY=2,5,1
12 *
13 *PLOT F(X)
14 *      WF=1E10:WM=0:WA=10^ACCURACY
15 *_NEW! WM=WM+1:WN=INT(WM*X):WDISS=WM*X-WN:IF WDISS<0.5 THEN CONT!
16 *      WDISS=1-WDISS:WN=WN+1
17 *_CONT! WB=WDISS/WN:WB=WN+WA*WB*WB:IF WF<=WB THEN TEST!
18 *      WF=WB:WMM=WM:WNN=WN
19 *_TEST! IF WN<WF THEN NEW!
20 *      Y=LOG(WF)
21 *_END
22 *
23 *

```



Some simple applications of editorial arithmetics: Any expression like  $2+2=_$  can be evaluated by moving the cursor to the position after  $=$  and by pressing the activation key COMMAND. The last example shows, how (after activation of  $FV=$ ) the system is able to find definitions and formulas from the edit field and how it calculates the activated expression on the basis of these formulas. Thus no 'program' in the normal sense is needed for these computations.

```
s 11 1 SURVO 84 EDITOR 07-22-1984 17:25:12 A: 100 72 31382 0
24 *Arithmetics:
25 *
26 *Arithmetics:
27 *
28 *      2+2=_ (23*17-67)/(1900-78)=
29 *
30 *      2+12=_ SQR(49)=
31 *
32 *      A=3 B=A+1 C=SQR(A*A+B*B) C+1=
33 *
34 *Computing compound interest:
35 *
36 *Let N be number of years,
37 *      PMT the present value,
38 *      FV the future value and
39 *      P the interest rate.
40 *Then  $FV=PMT \cdot r \cdot N$  where  $r=1+P/100$ .
41 *
42 *If N=10 , PMT=2000 and P=12 ,
43 *
44 *then FV=
45 *
46 *
```

```
s 9 1 SURVO 84 EDITOR 07-22-1984 17:33:49 A: 100 72 32232 0
24 *Arithmetics:
25 *
26 *Arithmetics:
27 *
28 *      2+2=4 (23*17-67)/(1900-78)=0.1778265642151482
29 *
30 *      2+12=4096 SQR(49)=7
31 *
32 *      A=3 B=A+1 C=SQR(A*A+B*B) C+1=6
33 *
34 *Computing compound interest:
35 *
36 *Let N be number of years,
37 *      PMT the present value,
38 *      FV the future value and
39 *      P the interest rate.
40 *Then  $FV=PMT \cdot r \cdot N$  where  $r=1+P/100$ .
41 *
42 *If N=10 , PMT=2000 and P=12 ,
43 *
44 *then FV=6211.696147918701
45 *
46 *
```

Evaluating formal derivatives of mathematical functions is a feature in SURVO 84 which enables making of more intelligent programs. For example, in nonlinear regression analysis the derivatives of the model function play an essential role.

```
■ 14 1 SURVO 84 EDITOR 07-22-1984 16:56:57 A: 100 72 31749 0
1 *SAVE DER
2 *
3 *DER <function of variable x>,<variable x>
4 *forms the analytical derivative of the function with respect to
5 *<variable x> and writes the result on the next two lines in the edit
6 *field. For example,
7 *
8 *DER (X+A)↑X X
9 *
10 *
11 *
12 *DER F(G(LOG(x)))
13 *
14 *
15 *
16 *DER SIN(G(t)/t) t
17 *
18 *
19 *
20 *SURVO 84 employs itself analytical derivatives in the ESTIMATE operation
21 *for linear and nonlinear regression models and for general Maximum
22 *likelihood problems.
23 *
```

```
■ 18 1 SURVO 84 EDITOR 07-22-1984 17:05:03 A: 100 72 32560 0
1 *SAVE DER
2 *
3 *DER <function of variable x>,<variable x>
4 *forms the analytical derivative of the function with respect to
5 *<variable x> and writes the result on the next two lines in the edit
6 *field. For example,
7 *
8 *DER (X+A)↑X X
9 * Derivative of (X+A)↑X with respect to X is
10 *      (X+A)↑X*(LOG(X+A)+X/(X+A))
11 *
12 *DER F(G(LOG(x)))
13 * Derivative of F(G(LOG(x))) with respect to x is
14 *      F'(G(LOG(x)))*G'(LOG(x))*1/x
15 *
16 *DER SIN(G(t)/t) t
17 * Derivative of SIN(G(t)/t) with respect to t is
18 *      COS(G(t)/t)*(t*G'(t)-G(t))/t↑2
19 *
20 *SURVO 84 employs itself analytical derivatives in the ESTIMATE operation
21 *for linear and nonlinear regression models and for general Maximum
22 *likelihood problems.
23 *
```

Linear and nonlinear regression models can be estimated by the ESTIMATE operation which is able to analyze the form of the model function by means of the derivatives. For example, when seeing that the second derivatives with respect to the unknown parameters are zero (as in the case we have here) the system knows that the model is linear and selects the numerical algorithm accordingly.

```

s 28 1 SURVO 84 EDITOR 07-22-1984 18:03:01 A: 100 100 29775 0
1 *SAVE EST
2 *
3 *DATA COUNTRIES,A,B,C
4 C Country Coffee Tea Beer Wine Spirits
5 *
6 A Italy 3.6 0.06 13.6 106.6 2.0
7 * Portugal 2.2 0.03 27.5 89.3 0.9
8 * Norway 9.4 0.19 43.5 3.1 1.8
9 * Spain 2.5 0.03 43.6 73.2 2.7
10 * France 5.2 0.10 44.5 104.3 2.5
11 * Finland 12.5 0.15 54.7 7.6 2.7
12 * Sweden 12.9 0.30 58.3 7.9 2.9
13 * Switzerland 9.1 0.25 73.5 44.9 2.1
14 * Holland 9.2 0.58 75.5 9.7 2.7
15 * England 1.8 3.49 113.7 5.1 1.4
16 * Denmark 11.8 0.41 113.9 10.4 1.7
17 B Ireland 0.2 3.73 124.5 3.8 1.9
18 *
19 *MODEL Beer1
20 *log(Beer)=constant+coeff*log(Tea)
21 *
22 *ESTIMATE COUNTRIES,Beer1,24
23 *

```

```

s 28 1 SURVO 84 EDITOR 07-22-1984 18:10:20 A: 100 100 29810 0
10 * France 5.2 0.10 44.5 104.3 2.5
11 * Finland 12.5 0.15 54.7 7.6 2.7
12 * Sweden 12.9 0.30 58.3 7.9 2.9
13 * Switzerland 9.1 0.25 73.5 44.9 2.1
14 * Holland 9.2 0.58 75.5 9.7 2.7
15 * England 1.8 3.49 113.7 5.1 1.4
16 * Denmark 11.8 0.41 113.9 10.4 1.7
17 B Ireland 0.2 3.73 124.5 3.8 1.9
18 *
19 *MODEL Beer1
20 *log(Beer)=constant+coeff*log(Tea)
21 *
22 *ESTIMATE COUNTRIES,Beer1,24
23 *
24 *Estimated parameters of model Beer1
25 *constant=4.488964 (.156575)
26 *coeff=.3276288 (7.527091E-02)
27 *Correlations:
28 *      consta coeff
29 *constant 1.000 0.687
30 *coeff 0.687 1.000
31 *RSS=1.553654 R2=.6545251
32 *

```

As an example of true nonlinear estimation problem, the location and the radius of a circle are determined on the basis of 20 points in the X-Y plane.

Firstly a data file is created and simulated data values generated. Then the least squares estimates for the parameters are computed by using model C starting from 'wrong' initial values.

```
# 14 1 SURVO 84 EDITOR 08-17-1984 15:17:06 A: 100 100 27264 0
1 *SAVE CIRCLE
2 *
3 *
4 *FILE CREATE CIRCLE,1,10,64,20
5 * 20 points (X,Y) approximately on the circumference of the circle
6 * (X-X0)^2+(Y-Y0)^2=R^2, where X0=5, Y0=6 and R=N(3,0.2^2)
7 *FIELDS:
8 * 1 N 4 X
9 * 2 N 4 Y
10 *END
11 *#####
12 *
13 *Generating 20 points (X,Y):
14 *
15 *VAR TO CIRCLE
16 *BASIC
17 *WR=%Normal(3,0.04)
18 *WT=%Uniform(0,6.2832)
19 *X=5+WR*COS(WT):Y=6+WR*SIN(WT)
20 *END
21 *#####
22 *
23 *
```

```
# 21 1 SURVO 84 EDITOR 08-17-1984 15:25:07 A: 100 100 27385 0
24 *
25 *MODEL C
26 *SQR((X-X0)^2+(Y-Y0)^2)=R
27 *
28 *INIT=4,5,2 / Initial values for X0,Y0,R
29 *ESTIMATE CIRCLE,C,30
30 *Estimated parameters of model C
31 *X0=5.005461 (7.120773E-02)
32 *Y0=6.028773 (8.152406E-02)
33 *R=2.903806 (5.650576E-02)
34 *Correlations:
35 *      X0      Y0      R
36 *X0      1.000  0.192  0.493
37 *Y0      0.192  1.000  0.234
38 *R       0.493  0.234  1.000
39 *RSS=.7994619
40 *
41 *
42 *
43 *
44 *
45 *
46 *
```

(Continuation)

Finally the data and two circles (one with initial values and another with estimated ones) are plotted.

```

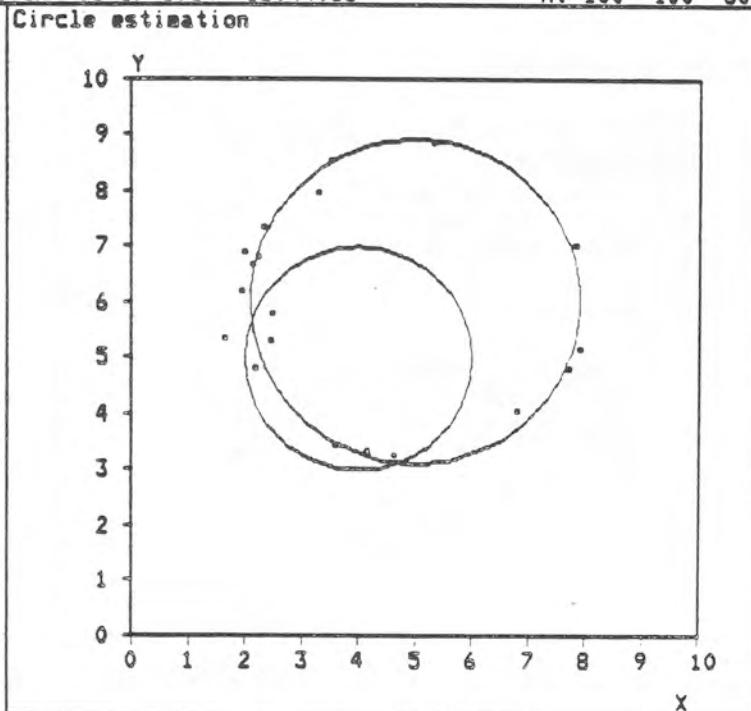
■ 39 1 SURVO 84 EDITOR 08-17-1984 15:33:03      A: 100 100 27364 0
24 *
25 *MODEL C
26 *SQR((X-X0)^2+(Y-Y0)^2)=R
27 *
28 *INIT=4,5,2 / Initial values for X0,Y0,R
29 *ESTIMATE CIRCLE,C,30
30 *Estimated parameters of model C
31 *X0=5.005461 (7.120773E-02)
32 *Y0=6.028773 (8.152406E-02)
33 *R=2.903806 (5.650576E-02)
34 *Correlations:
35 *      X0      Y0      R
36 *X0      1.000  0.192  0.493
37 *Y0      0.192  1.000  0.234
38 *R       0.493  0.234  1.000
39 *RSS=.7994619
40 *
41 *HEADER=Circle_estimation
42 *XSCALE=0(1)10 YSCALE=0(1)10
43 *PLOT CIRCLE,X,Y
44 *PLOT X(T)=4+2*COS(T),Y(T)=5+2*SIN(T)
45 *PLOT X(T)=X0+R*COS(T),Y(T)=Y0+R*SIN(T)
46 *T=0,6.2832

```

```

■ 1 1 SURVO 84 EDITOR 08-17-1984 15:44:55      A: 100 100 30120 0

```



The matrix interpreter of SURVO 84 permits various matrix operations to be performed in the edit field.  
In this example a 4x4 matrix A is inverted.

```
■ 11 1 SURVO 84 EDITOR 07-22-1984 18:42:52 A: 100 100 28947 0
1 *SAVE MAT
2 *      Matrix operations in SURVO 84
3 *
4 *Computing inverse of A:
5 *
6 *MATRIX A ///
7 *      12.5  4.2  11.0 -8.1
8 *      0.0   -1.3  5.6   2.4
9 *      5.2   10.4 -9.3   0.3
10 *     1.0    3.5  2.4  12.9
11 *
12 *MAT SAVE A
13 *MAT B=INV(A)
14 *MAT LOAD B,16
15 *
16 *
17 *
18 *
19 *
20 *
21 *
22 *
23 *
```

```
■ 1 1 SURVO 84 EDITOR 07-22-1984 18:52:03 A: 100 100 29031 0
1 *SAVE MAT
2 *      Matrix operations in SURVO 84
3 *
4 *Computing inverse of A:
5 *
6 *MATRIX A ///
7 *      12.5  4.2  11.0 -8.1
8 *      0.0   -1.3  5.6   2.4
9 *      5.2   10.4 -9.3   0.3
10 *     1.0    3.5  2.4  12.9
11 *
12 *MAT SAVE A
13 *MAT B=INV(A)           / *B~INV(A) 4*4
14 *MAT LOAD B,16
15 *
16 *MATRIX B
17 *INV(A)
18 *///
19 * 1      0.1776 -0.9609 -0.2918  0.2971
20 * 2      -0.1268  0.9541  0.3560 -0.2654
21 * 3      -0.0416  0.5206  0.1242 -0.1259
22 * 4      0.0284 -0.2812 -0.0971  0.1499
23 *
```

Canonical analysis on two sets of variables X,Y on the same observations is performed by using a series of MAT operations. Observe that the computations are essentially based on the singular value decomposition. The results are loaded at the end of the of the operations. This is an example of a 'matrix program' for multivariate statistical analysis.

```

■ 17 1 SURVO 84 EDITOR 07-22-1984 19:03:21 A: 100 100 26930 0
24 *
25 * Canonical correlations
26 *
27 *MAT X'=CENTER(X)           / *X!~CENTER(DECA) 48*5
28 *MAT Y!=CENTER(Y)          / *Y!~CENTER(DECA) 48*5
29 *MAT GRAM-SCHMIDT DECOMPOSITION OF X TO QX,RX
30 *MAT GRAM-SCHMIDT DECOMPOSITION OF Y TO QY,RY
31 *MAT H=QX'                 / *H~GS(X)' 5*48
32 *MAT H=H*QY                / *H~GS(X)'*GS(Y) 5*5
33 *MAT SINGULARVALUE DECOMPOSITION OF H TO U,LAMBDA,V
34 *MAT SOLVE ALPHA FROM RX*ALPHA=U   / *Upper triangular
35 *MAT SOLVE BETA  FROM RY*BETA=V   / *Upper triangular
36 *MAT ALPHA!=NRM(ALPHA)        / *ALPHA!~NRM((ALPHA_from_RX*ALPHA=U)) 5*5
37 *MAT BETA!=NRM(BETA)         / *BETA!~NRM((BETA_from_RY*BETA=V)) 5*5
38 *MAT LAMBDA=VD(LAMBDA)       / *LAMBDA~VD(Qsvd(GS(X)'*GS(Y))) 5*1
39 *MAT LAMBDA!=LAMBDA'        / *LAMBDA!~LAMBDA 1*5
40 *MAT LOAD LAMBDA,END+2
41 *MAT LOAD ALPHA,END+2
42 *MAT LOAD BETA,END+2
43 *
44 *
45 *
46 *Results on the next page!

```

```

■ 1 1 SURVO 84 EDITOR 07-22-1984 19:15:59 A: 100 100 28623 0
47 *
48 *MATRIX LAMBDA
49 /**/      U1      U2      U3      U4      U5
50 *Diag    0.7894  0.5284  0.3306  0.2823  0.0972
51 *
52 *MATRIX ALPHA
53 /**/      U1      U2      U3      U4      U5
54 *100m   -0.4631  0.7126  0.3823  0.3025  0.2574
55 *Br_jump -0.1403  0.4297 -0.6201 -0.4593 -0.2937
56 *Shot_put -0.7471 -0.3920 -0.2396  0.2995 -0.1706
57 *Hi_jump -0.1805  0.1065 -0.0784 -0.0724  0.8592
58 *400m    0.4185 -0.3775 -0.6370  0.7763  0.2830
59 *
60 *MATRIX BETA
61 /**/      V1      V2      V3      V4      V5
62 *Hurdles -0.1200  0.3912 -0.7545  0.4979 -0.1728
63 *Discus   -0.8919 -0.6855 -0.2195  0.1943 -0.4581
64 *Pole_vlt 0.0837  0.1561  0.0024 -0.2574 -0.8142
65 *Javelin  0.1444  0.0004 -0.5062 -0.7343  0.0691
66 *1500m   0.4028 -0.5938 -0.3555  0.3301 -0.3043
67 *
68 *
69 *

```

The SURVO 84 matrix interpreter also provides operations for large supermatrices. In this example a 100\*100 matrix consisting of 25\*25 parts is inverted. The matrix has a simple structure: All diagonal elements are 1 and other elements are 0.8. The structures of the supermatrices R%, S% are given in the edit field and the parts A,B are formed by MAT operations. Finally R% is inverted by MAT S%=INV(R%). After inversion the result is examined and compared with known theoretical values.

```
■ 15 1 SURVO 84 EDITOR 08-18-1984 11:27:54 A: 100 100 26679 0
1 *
2 * Inverting partitioned 100*100 matrix
3 *MATRIX R%
4 *A B B B
5 *B A B B
6 *B B A B
7 *B B B A
8 *
9 *MATRIX S%
10 *S11 S12 S13 S14
11 *S21 S22 S23 S24
12 *S31 S32 S33 S34
13 *S41 S42 S43 S44
14 *
15 *n=25 r=0.8 s=0.2
16 *
17 *MAT B=CON(n,n)
18 *MAT B!=r*B / *B!((B S25*25
19 *MAT A=IDN(n)
20 *MAT A=s*A / *A<(s*I D25*25
21 *MAT A!=A+B / *A!((A S25*25
22 *MAT S%=INV(R%)
23 *
```

```
■ 44 1 SURVO 84 EDITOR 08-18-1984 11:36:18 A: 100 100 28721 0
25 *#####
26 *n=25 r=0.8 N=4*n
27 *x=(1+(N-2)*r)/q q=1+(N-2)*r-(N-1)*r*r
28 *y=-r/q
29 *x=4.950124688279302
30 *y=-4.9875311720698260-02
31 *
32 *MAT LOAD S11(1:3,1:3),##.#####,33
33 *MATRIX S11
34 *INV(A)-INV(A)*B*INV(A-B*INV(A)*B)*(-B*INV(A))-(INV(A)*B-INV(A)*B*INV(A-B*
35 */// 1 2 3
36 * 1 4.950124688279277 -0.049875311720723 -0.049875311720723
37 * 2 -0.049875311720723 4.950124688279277 -0.049875311720723
38 * 3 -0.049875311720722 -0.049875311720723 4.950124688279278
39 *
40 *MAT LOAD S44(1:3,1:3),##.#####,41
41 *MATRIX S44
42 *INV(A-B*INV(A)*B)-(B-B*INV(A)*B)*INV(A-B*INV(A)*B)*(B-B*INV(A)*B)-(B-B*INV
43 */// 1 2 3
44 * 1 4.950124688279299 -0.049875311720701 -0.049875311720701
45 * 2 -0.049875311720701 4.950124688279299 -0.049875311720701
46 * 3 -0.049875311720701 -0.049875311720701 4.950124688279299
47 *#####
```